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| <b>Description: Clip 2 of 5: Investigating the Number of Shortest Paths</b><br><b>Parent Tape: Taxicab Geometry</b><br><b>Date: 2000-05-05</b><br><b>Location: David Brearley High School</b><br><b>Researcher(s): Professor Carolyn Maher</b> | <b>Transcriber(s): Powell, Arthur; Milonas, Jeremy</b><br><b>Verifier(s): McGowan, Will; Brookes, Elijah</b><br><b>Date Transcribed: Spring 2010</b><br><b>Page: 1 of 7</b> |
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| 1  | 00:14:25 | JEFF   | All right. So-   |
| 2  |          | ROMINA | Pick a dot.  |
| 3  |          | JEFF   | Right there.   |
| 4  |          | ROMINA | One, two.  |
| 5  |          | JEFF   | Two. All right. Here.  |
| 6  |          | T/R2   | We also have more to choose from.  |
| 7  |          | JEFF   | Jesus.   |
| 8  |          | T/R2   | There's graph paper there. Okay  |
| 9  |          | ROMINA | Okay. So one, two, three- Oh, is this going to be dumb and stuff? One, two, three, four- It looks like a multiplication table. (00   |
| 10 |          | JEFF   | All right. Uh, one-, two [Inaudible]. [Brian draws his eighth symbol on the right side of the grid and writes "1, 4, 2." On the top of "1, 4, 2" he writes "DRD." He also goes back to 7 and writes "D3, R1". He has written a number with each of the first 6 symbols on Brian's paper, too.] |
| 11 |          | ROMINA | All right.   |
| 12 |          | JEFF   | Why don't you just- here, use blue. It doesn't matter.   |
| 13 |          | ROMINA | Yeah. One-   |
| 14 | 00:15:30 | JEFF   | One- //two.  |
| 15 | 00:22:52 | ROMINA | Mm hmm. Or you go all the way top to bottom.   |
| 16 |          | JEFF   | There's nothing else to do? Right? Now that would be the opposite of that one. That would be the opposite of that one and that would be the opposite of that one. //They're all covered. [Pointing to pairs of routes on the grid with a pen.]   |
| 17 |          | ROMINA | //So we got six. Good. Good thing we did that over again. (00  |
| 18 |          | JEFF   | All right, well. Yeah, good because at least we're- you know, //we're- we're making  |

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|    |  |              | progress. [Romina writing 6 on her transparency of centimeter paper in the square that represents a two-by-two grid.]  |
| 19 |  | ROMINA       | //Yeah, all right. And go-   |
| 20 |  | JEFF         | All right. //The three-  |
| 21 |  | ROMINA       | //Three and two. [Jeff draws three vertical lines, creating four three-by-two rectangles.]   |
| 22 |  | JEFF         | The greatest MC in the world. [Singing.] Look at that. Beautiful. [Drawing three-by-two rectangles on the grid and crossing out the others]  |
| 23 |  | ROMINA       | Tell me you know how to count those. All right. [Jeff crossing out the 6 different 2 by 2s he just drew shortest routes on.]   |
| 24 |  | JEFF         | All right. We can go like this, and that's the only way- [Drawing the one 2-down, 3-across route.]   |
| 25 |  | ROMINA       | Right.   |
| 26 |  | JEFF         | -to do that.   |
| 27 |  | ROMINA       | You want-, you want to do them in couples? (00   |
| 28 |  | JEFF         | Now the opposite of that is that right there. So that's that covers those two. [Underneath the previous route, drawing the one three-over route.] Now, the other way- now we've got to go one down like that. [Using a red marker to draw a route one-down, three-over.] And the couple of that would be- //I'm not- |
| 29 |  | ROMINA       | //[Inaudible].   |
| 30 |  | JEFF         | -not exactly sure so wait.   |
| 31 |  | ROMINA       | We can't go in couples I mean.   |
| 32 |  | JEFF         | Yeah well-   |
| 33 |  | ROMINA       | All right, I'm going to open the windows.  |
| 34 |  | JEFF         | Ah yeah? [Draws 2 more one-down routes in his 3-by-2 grids.]   |
| 35 |  | Cameraperson | What's making noise here? [Inaudible]?   |

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| 36 |  | ROMINA       | [Inaudible].  |
| 37 |  | Cameraperson | I understand.   |
| 38 |  | JEFF         | All right.  |
| 39 |  | ROMINA       | What'd you get?   |
| 40 |  | JEFF         | I don't know. I'm waiting for you, man.   |
| 41 |  | ROMINA       | All right. One, two-  |
| 42 |  | JEFF         | All right. That's that- [With his pen, pointing at the different three-by-two routes on the grid in which the first move is one down.]  |
| 43 |  | ROMINA       | Mm hmm.   |
| 44 |  | JEFF         | And that's that. And then, you know, that's going one over. It's going two over. It's going //three over.   |
| 45 |  | ROMINA       | //Three over.   |
| 46 |  | JEFF         | That covers all going through the middle.   |
| 47 |  | ROMINA       | Mm hmm.   |
| 48 |  | JEFF         | Correct?  |
| 49 |  | ROMINA       | Yes.  |
| 50 |  | JEFF         | All right. So now we've got to start going to the top. You can go one over, down, over. You can go one over or two over, down. You could also go one over, down two and over. You could also go- [Drawing the route.] |
| 51 |  | ROMINA       | We've got eight so far, right?  |
| 52 |  | JEFF         | Could also go, um, two over, two down and over. [Draws the route.]  |
| 53 |  | ROMINA       | Mm hmm.   |
| 54 |  | JEFF         | Anything else? That's one, two, three, four, five, six, seven, eight, nine. Oh, it's nine because that one doesn't have a couple.   |
| 55 |  | ROMINA       | Yeah, //okay.   |
| 56 |  | JEFF         | //Those are couples, uh, this one and that one are couples, uh- [Pointing to routes and matching them with marker.]   |
| 57 |  | ROMINA       | //The one going-  |
| 58 |  | JEFF         | //These two are couples. [Pointing with   |

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|    |          |         | marker.]   |
| 59 |          | ROMINA  | The one going all the way across in the middle is never going to have a //couple.  |
| 60 |          | JEFF    | //Never going to have a couple.  |
| 61 |          | ROMINA  | Because-   |
| 62 |          | JEFF    | That's- //so that will always be odd.  |
| 63 |          | ROMINA  | //All right, so you can't [Inaudible].   |
| 64 |          | JEFF    | So every other one will be odd because there will be one going fully across the middle. Right? That's why that's nine.   |
| 65 |          | ROMINA  | Well that can't be odd because it's-   |
| 66 |          | JEFF    | Hey- 'cause that- that won't-  |
| 67 |          | ROMINA  | Maybe any one with an odd length or width.   |
| 68 |          | JEFF    | Which would be every other one.  |
| 69 | 00:24:15 | ROMINA  | Yeah.  |
| 70 | 00:34:00 | JEFF    | Nah, there's one after that. So, if we could get to there it would be, uh, big time you know what I'm saying?  |
| 71 |          | ROMINA  | It's this one.   |
| 72 |          | JEFF    | This one right here?   |
| 73 |          | ROMINA  | Mm hmm.  |
| 74 |          | JEFF    | Three by-  |
| 75 |          | ROMINA  | Yeah.  |
| 76 |          | JEFF    | All right, well we're on- what are we on? Two by four? [Brian writing rows of numbers 0, 1, 2 or 3 silently. Michael has routes drawn all over his paper. He continues working.] |
| 77 |          | ROMINA  | Mm hmm. That's not going to be enough.   |
| 78 | 00:35:00 | JEFF    | That's all right. We can make more.  |
| 79 | 00:37:00 | JEFF    | You got that?  |
| 80 |          | BRIAN   | Man, I'm giving up on it.  |
| 81 |          | ROMINA  | Hum, that's kind of weird.   |
| 82 |          | BRIAN   | Mike here's the list. So far I've got some of the things [Inaudible].  |
| 83 |          | MICHAEL | How many have you got there, thirty?   |
| 84 |          | BRIAN   | No that's only like //[Inaudible].   |

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| 85  |          | JEFF    | //I think- I think we should like [inaudible] on like the next one we do, I think we should just like //do all ones over one. [Motioning across with his pen.] |
| 86  |          | BRIAN   | //D's is like down- //down one.  |
| 87  |          | JEFF    | //All those, you know what I'm saying?   |
| 88  |          | BRIAN   | Like the order.  |
| 89  |          | JEFF    | What else? Is there anything else?   |
| 90  |          | ROMINA  | No.  |
| 91  |          | JEFF    | That should be it.   |
| 92  |          | ROMINA  | That looks nice too, what they're doing.   |
| 93  |          | JEFF    | What?  |
| 94  | 00:37:35 | ROMINA  | Brian, see that looks like a much- when you do like the-   |
| 95  | 00:43:02 | MICHAEL | Huh?   |
| 96  |          | ROMINA  | three over and two down.   |
| 97  |          | JEFF    | One, two- Uh, that's [Inaudible].  |
| 98  |          | ROMINA  | Couldn't we just do something like in towers where like lines over are like the color and the lines down are the, um, number of blocks?                        |
| 99  |          | JEFF    | All right. And that would?   |
| 100 |          | ROMINA  | Because, okay, lines over- because what is it- the number of blocks to the number of colors?   |
| 101 |          | JEFF    | I don't know what you're- what- what's that?   |
| 102 |          | ROMINA  | Two to the $n$ . Two is the amount of blocks or the colors? (00  |
| 103 |          | MICHAEL | For what? Like towers on them?   |
| 104 |          | ROMINA  | Yeah.  |
| 105 |          | JEFF    | Colors. $n$ is the number of blocks. I think. I don't know. I'm not sure.  |
| 106 |          | MICHAEL | Well you figure a block has this- you got two-two towers over like this. Or two colors actually. I think it's, uh, the colors and $n$ is the blocks.           |
| 107 |          | ROMINA  | Color two- //right. [Writing the words "color" and "blocks" on a piece of paper.]  |

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| 108 | JEFF    | //Same thing.   |
| 109 | ROMINA  | All right, here we have one color- nah; it doesn't work for the first one.  |
| 110 | ROMINA  | Scratch that idea. [Crossing out the words on her paper.]   |
| 111 | JEFF    | Well- why- you know, what happened to the- to what we were doing?   |
| 112 | ROMINA  | No, I know. Just keep on going. [Jeff, Brian and Michael working silently.]   |
| 113 | JEFF    | All right.  |
| 114 | ROMINA  | You're right [inaudible] three by two.  |
| 115 | JEFF    | Can you help me out?  |
| 116 | ROMINA  | What- what [Inaudible] //by two of this sheet?  |
| 117 | BRIAN   | //That's what I got so far.   |
| 118 | ROMINA  | //You need one [Inaudible]?   |
| 119 | BRIAN   | //That's how far right there. It's on the board.<br>//The board.  |
| 120 | ROMINA  | //I know, I'm looking for- [Jeff continuing to draw routes.]  |
| 121 | BRIAN   | Mike do you see anything that I'm not getting?  |
| 122 | ROMINA  | //Three by three.   |
| 123 | MICHAEL | //Which one you doing?  |
| 124 | BRIAN   | Two by three.   |
| 125 | ROMINA  | Three by two. All right, here. This is what we got.   |
| 126 | JEFF    | It's really hot in here.  |
| 127 | ROMINA  | All right, we got down two over three. Over three, down two. [Brian drawing routes on the chalkboard while Romina reads off her possibilities.] |
| 128 | BRIAN   | //Okay.   |
| 129 | ROMINA  | //That's one of those? The first one.   |
| 130 | BRIAN   | It's like four moves.   |
| 131 | ROMINA  | All right we got those. [Brian continues writing on the chalkboard.] Got down one over three.   |
| 132 | ROMINA  | Except they don't have one, one, one, one, one,   |

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|     |          |        | that one.  |
| 133 |          | JEFF   | That's one we don't have?  |
| 134 |          | ROMINA | We don't have his last one over there. Check. I think that was the only one. So that nine does equal ten. [Brian writing, "start over" on the chalkboard and the word "Moves" up top.] |
| 135 |          | JEFF   | I don't see uh- Um- two, four, six, eight...   |
| 136 |          | ROMINA | Because we don't have that one?  |
| 137 |          | JEFF   | No, we don't have that one. [Inaudible]. [Romina erases the 9s and writes in 10s. She also writes a 5 under the 4.]  |
| 138 | 00:46:46 | ROMINA | All right. It's, um, - it's Pascal's triangle. [Looking at the numerical array of the 1-centimeter-grid transparency.]   |