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Description: Placing Numbers on the Big Number Line
(clip 4 of 4)
Parent Tape: Number Line Models and Placing Numbers
on the Big Number Line
Date: 1993-11-10
Location: Colts Neck Elementary School
Researcher: Professor Carolyn Maher
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| Line | Time | Speaker | Transcription |  |
| :---: | :--- | :--- | :--- | :--- |
| 1. |  | RT1 | Okay, we only have about fifteen minutes so I would like to try something else. <br> [Directed to the group at the overhead.] Thank you very much girls, I appreciate <br> that. [Groups sits down. RT1 rearranges front of room.] What do you think we <br> are going to do now? |  |
| 2. |  | Students | Fill in that number board. |  |
| 3. |  | RT1 | We are going to fill in the number line, that is right. Are you <br> all thinking of your numbers? |  |
| 4. |  | Students | Oh. No. [Giggles] | Okay, now remember someone else may take your number so you had better have <br> a few extra numbers ready to go and place them on that number line and if indeed <br> we find that some of you disagree, then you will have to argue why you are <br> placing it. Maybe someone will convince you to change your it or maybe you <br> will convince them that you will not change it, Okay? |
| 5. |  | RT1 |  |  |
| 6. |  | Jessica | [Jessica speaks softly off camera.] |  |
| 7. |  | RT1 | That is a very good question, Jessica says let's have some ground rules, that's <br> right. In other words, if we were going to put three thirds we are going to go <br> underneath? Right? Where would you put it? |  |
| 8. |  | Students | On top. |  |
| 9. |  | RT1 | Well, let's try to put it underneath; if we come out of room, then maybe we'll try <br> to figure out another way. Is that fair? |  |
| 10. |  | Students | Um-Hun. [Yes.] |  |
| 11. |  | RT1 | If we have different names for the same number, that might be interesting. We <br> could put them underneath. Brian? |  |


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| 12. |  | Brian | Should we go from zero to one? |  |
| ---: | :--- | :--- | :--- | :--- |
| 13. |  | RT1 | No, we are going zero to, by the way we have to thank Mrs. Deming for making <br> us this number line. She is running the camera back there. We could keep <br> making it bigger. I do not know if Colt's Neck will let us break through the walls <br> or we could go on the other side of the walls. Mrs. Deming assures us that if you <br> want to keep enlarging this number line, that is fine. Okay? So we could have <br> some fun with this. Are you all ready? I'll take volunteers. I'd like to hear from <br> some people that have not been up yet, so I'd like some volunteers. There are <br> some advantages to volunteering early. Do we have some volunteers? [Three <br> students raise their hands.] Come on Audra. Jessica are you volunteering? Does <br> someone have a ruler that might help mark the line? [Audra brings up a ruler.] <br> All eyes are on Audra to see what she will pick. [Audra writes one half under the <br> zero.] |  |
| 14. |  | Michael | No. That's not right. She puts one half on the zero. That is half between <br> negative and positive, but that is not a half on the number line. Yeah. |  |
| 15. |  | Students | [Students discuss what Audra did.] |  |
| 16. | Alan | She is putting a half there we have three negative and three positive numbers, she <br> is using negative three as the beginning of the line and the positive three as the <br> end. |  |  |
| 17. |  | Brian | It should be one half between zero and three because on that side is the negative <br> side. |  |
| 18. |  | RT1 | Bryan thinks it should go between the zero and the three. |  |
| 19. |  | A Student | [Off camera] I do, too. |  |
| 20. |  | Alan | I think she is right. |  |
| 21. |  | A Student | I don't think so because its at the end. |  |

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| 36. |  | RT1 | Alan? |  |
| :--- | :--- | :--- | :--- | :--- |
| 37. |  | Alan | Since you added on the four, then, that mean you now have four numbers positive <br> but three numbers negative |  |
| 38. |  | RT1 | By the way, do I really have four numbers positive? |  |
| 39. | Students | You have four numbers negative. You have five numbers positive ... zero, one, <br> two, three, and four. |  |  |
| 40. |  | RT1 | Is that what we have on the number line? Numbers up to four? |  |
| 41. | Students | [Murmur. $]$ |  |  |
| 42. | Audra | This can't be one half. |  |  |
| 43. | RT1 | Okay. Let me ask all of you a question. Does that number line end at four? |  |  |
| 44. | Students | No. |  |  |
| 45. |  | RT1 | Does it end at five? |  |
| 46. |  | Students | No. |  |
| 47. |  | RT1 | Where does it end? |  |
| 48. |  | Students | Nowhere. It keeps on going. Infinity. |  |
| 49. | RT1 | Where does it end on the other side? |  |  |
| 50. | Students | Nowhere. Infinity. | But, I should be able to place every single one of my numbers and, just because I <br> have run out of room to write it, that should not get in our way; we have to <br> imagine these numbers going on. I would like to know where I would put <br> negative one half. |  |
| 51. | RT1 |  |  |  |
| 52. |  | Students | Negative one half? |  |
| 53. |  | Student | [Off camera You have to have an even number. |  |

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| 54. | Alan | All negative numbers are different than positive. [Stands up and comes to the board to point.] From here down you are negatives so that means any number here cannot be equivalent to a number over there, so that means if you were dividing this part up into fractions, you would have to put one half mark in the negative, right about there. |  |
| :---: | :---: | :---: | :---: |
| 55. | RT1 | So, you would put a negative one half between negative one and negative two? |  |
| 56. | Students | Yeah. |  |
| 57. | RT1 | What do you think about that Meredith? |  |
| 58. | Meredith | Because one and one and one half and one half is three. |  |
| 59. | RT1 | Where would you put three-quarters? |  |
| 60. | Students | Negative or positive? |  |
| 61. | RT1 | Positive three-quarters. |  |
| 62. | Erik | Positive three-quarters, that is simple. |  |
| 63. | RT1 | I am confused. Yeah, let us hear what Meredith has to say. Why don't you all sit down. [Meredith walks up to board.] |  |

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| 64. |  | Meredith | If you are asking where is three fourths, three fourths would be here, here, and <br> here. This would be one-quarter, this would be two-quarters, this would be three- <br> quarters, and this would be four-quarters. <br> This would be one and one-quarter, this would be one and two-quarters. <br> This would be one and three-quarters, this would be one and four-quarters. This <br> would be two and so on. |  |
| ---: | :--- | :--- | :--- | :--- |
| 65. |  | RT1 | I am still confused now why one half is on the zero? And, why two quarters is <br> between zero and one? I am very confused. |  |
| 66. |  | Meredith | If you have zero to one, it would not be from zero to four. You would not divide <br> it like that. You would divide it one fourth, two fourths, three fourths, four <br> fourths. This would be one and one fourth, one and two fourths, one and three <br> fourths, two. |  |
| 67. |  | RT1 | Thank you very much Meredith. How many of you agree with what Meredith <br> did? How many agree? It makes sense to you? |  |
| 68. | Students | [All students on camera raise their hand.] |  |  |
| 69. | RT1 | Everybody in this class agrees. Okay. Everyone agrees. I am still a little <br> confused with where to put one half. I am very confused. Can you understand <br> that I am confused? You want to keep it there Meredith? Do not tell me where to <br> put it. |  |  |
| 70. |  | Meredith | No. |  |
| 72. |  | RT1 | Sow many of you want to keep it there? |  |
| 73. | Students | RT1 | RNo one on camera raise their hand.] No. | How many of you want to put it some where else? |

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| 74. | Students | [Ten students on camera raise their hand.] |  |
| :---: | :---: | :---: | :---: |
| 75. | RT1 | Amy? |  |
| 76. | Amy | You could keep it there, but you have to add negative four. |  |
| 77. | Students | You have to do something to keep it there. |  |
| 78. | RT1 | David? |  |
| 79. | David | I think Audra is using the whole thing while Meredith is using from zero to two. |  |
| 80. | Alan | When adding up all those numbers on the negative side would just be like doing nothing. |  |
| 81. | RT1 | I'm kind of curious where Meredith would put negative one fourth? Negative two fourths? Negative three fourths? and negative four fourths? I am kind of curious where she would do that. |  |
| 82. | Meredith | [Walks up to board.] |  |
| 83. | Students | She is like cutting the number line. |  |
| 84. | RT1 | I am still very confused about where that one half is. I do not know how zero and one half could be the same point. Very confusing to me. If we are given a point with the number name zero, I don't see how it could have another number named one half. I am so confused. I hope you will straighten me out, because I am so confused. |  |
| 85. | Meredith | It doesn't. |  |
| 86. | David | When you put one more number, four. Before it was from negative three to three, when it was from negative three to three so zero was one half. But, now that you added the four to the positive side it is not one half, both sides of the negative and positive are not equivalent. |  |

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| 87. |  | RT1 | But, you told me earlier that I could put four fourths here because that is another <br> name for one. And, I think some of you told me that I could put five fifths here <br> because that is another name for one. And, in fact, I thought I even heard <br> Michael say earlier that you could put a thousand thousandths here because that is <br> another name for one. Did you say that Michael? |  |
| ---: | :--- | :--- | :--- | :--- |
| 88. |  | Michael | Um-Hun [Yes.] You could put a million millionths there. |  |
| 89. |  | RT1 | You could put million millionths. And, you could put other names for one here. <br> But, I don't understand how another name for zero could be one half. I am so <br> confused; this mathematics is confusing to me. James? |  |
| 90. |  | James | I think that one half might go between zero and one. Half of it is negative one, <br> negative two, negative three. The other half is one, two, three, four. |  |
| 91. |  | RT1 | Do you want to show us what you are thinking? [RT1 passes the marker to <br> James.] That is an interesting idea. You can write it underneath on the bottom. <br> So am I hearing James say that one half is another name for two fourths? |  |
| 92. |  | Students | [Murmur] Um-Hum. |  |
| 93. |  | RT1 | What do you think, is that possibility? |  |
| 94. |  | Students | Yeah. | Thank you James. What do you think about what James did? That one half is <br> another name for two fourths? |
| 95. | RT1 |  |  |  |
| 96. |  | OHP | Yeah. |  |
| 97. |  | Students | Ye |  |
| 98. |  | RT1 | Audra? |  |
| 99. |  | Audra | I agree because [inaudible].... even fractions so that ... [inaudible].... |  |
| 100. |  | RT1 | Am I hearing you change you mind? |  |

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| 101. | Audra | [inaudible $]$ |  |  |
| ---: | :--- | :--- | :--- | :--- |
| 102. | RT1 | Audra is telling me that one half could go here. Can zero and one half be the <br> same? How do you feel about that? Not sure? Want to think about that? |  |  |
| 103. | Audra | Well, one half could be anywhere between these number. one half could be <br> between ... [inaudible] |  |  |
| 104. | RT1 | Could someone tell me what the confusion is? There is clearly something that we <br> are getting confused about. Andrew, and, then, James. |  |  |
| 105. | Andrew | I think what we are all getting confused about is the length of the number line. <br> We have five positive number and four negative numbers counting the zero. <br> They are not exactly the same so you would have to put one half a little more <br> over to the positive side where two fourths is, now that we have three negative <br> number and four positive numbers. |  |  |
| 106. | RT1 | How many agree that is what the confusion is? |  |  |
| 107. | Students | [Mumbles.] No. | How many think there is something else that is the <br> confusion? James? | I think the confusion is one half is in the middle of two things. So, it is confusing <br> to see in which place between three to four, two to three, one to two, zero to one, <br> negative one to zero, negative two to negative one. I think that is the confusion. |
| 109. | James | Would you place one half here would you place number one half here [Points to <br> the middle of two and three on the number line]? |  |  |
| 110. | RT1 |  |  |  |
| 111. |  | Students | Yeah. |  |

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| 112. | RT1 | We are talking about the number one half. I am asking you the question. I agree <br> that you could find the one half the length between two and three, I agree, but <br> could place the number one half here? |  |  |  |
| ---: | :--- | :--- | :--- | :--- | :--- |
| 113. | Meredith | [Exclaims] It has to be two and one half. |  |  |  |
| 114. | RT1 | Is that allowed? Andrew? |  |  |  |
| 115. | Andrew | It has to be two and one half. | You could put two and one half here, I could take this and split it in one half but I <br> would not put one half here, I would put two and one half. Agree? |  |  |
| 116. | RT1 | Brian | You could be a one half between every number....like <br> [Gets up and runs up to board.] |  |  |
| 117. |  | RT1 | That's okay, Brian, we can hear you. [Motions to Bryan to sit down.] <br> 118. | Between the zero and the one would be a one half. Between the one and the two <br> would be one and one half. Between two and three would be two and one half. <br> Between three and four would be three and one half and the same on the negative <br> side. |  |
| 120. | RT1 | Okay. How many agree with that? In another words you are saying that the one half you are <br> splitting that and then you know where to place those numbers. You were all telling me to place <br> the number one half on the zero. I got very confused. What are they thinking, Alan? |  |  |  |
| 121. | Alan | They were thinking negative numbers are equal to positive numbers. That is <br> probably what they are thinking. Because, you cannot add negative numbers and <br> have them be positive numbers. |  |  |  |
| 122. |  | Brian | Audra was thinking all that is 1 whole and its not. |  |  |
| 123. | Alan | The negative numbers are lower than zero. Zero is said to be the lowest number <br> and they are lower than the lowest. |  |  |  |

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| 124. | RT1 | Okay. We have about 1 more comment and we will continue this when we come <br> back. Meredith? |  |  |
| ---: | :--- | :--- | :--- | :--- |
| 125. | Meredith | It is like a ruler, here it has the inches one half, one and one half, two and one <br> half, three and one half, four and one half, five and one half, |  |  |
| 126. |  | and so on. [Holds up a ruler and points to the tics.] |  |  |
| 127. | RT1 | It is starting to make some sense? |  |  |
| 128. | Students | [Murmur] Ohm-Hum |  |  |
| 129. | RT1 | Audra, I am so glad you placed one half there; it ended up in such a good <br> discussion. Are we going to leave it there or take that one half off? |  |  |
| 130. | Students | Take it off! | You want it off over there. Should we continue this tomorrow? We'll continue <br> this Friday. We are going to Rutgers tomorrow. Have a wonderful day. You <br> were all wonderful. |  |
| 131. | RT1 |  |  |  |

