Description: Early Algebra Ideas About Binomial Expansion, Stephanie's Interview Two of Seven: Clip 6 of 6, The square of $(a+b)$, how to imagine each piece?
Parent Tape: Early Algebra Ideas About
Binomial Expansion, Stephanie's Interview
Two of Seven
Date: 1996-01-29
Location: Harding Elementary School Researcher: Carolyn A. Maher

Transcriber(s): Aboelnaga, Eman
Verifier(s): Yedman, Madeline
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| Line | Time | Speaker | Transcript |
| :---: | :---: | :---: | :---: |
| 1 |  | R1 | $a$ squared. In your head, do you know what you're imagining here? In this piece? [indicates the lower left corner of the $(a+b)^{2}$ model Stephanie drew] |
| 2 |  | Stephanie | Well, it's just this square would be $a$. |
| 3 |  | R1 | Right. |
| 4 |  | Stephanie | It would just be like this piece right here. [Stephanie traces the $a^{2}$ section of the model.] |
| 5 |  | R1 | Tell me about this piece. What does this $a$ squared mean for this piece? |
| 6 |  | Stephanie | It means that that's like the area of the piece. |
| 7 |  | R1 | Right. But what am I supposed to imagine in my piece. |
| 8 |  | Stephanie | There's $a$ squared number of units uh square units. |
| 9 |  | R1 | Okay. |
| 10 |  | Stephanie | In there. |
| 11 |  | R1 | And what's the length of one? |
| 12 |  | Stephanie | One. |
| 13 |  | R1 | Okay. So you have two, three, four, five, dot, dot, dot [marks off intervals along the left side of the $a^{2}$ section]. |
| 14 |  | Stephanie | Um hm. |
| 15 |  | R1 | Each of these is one. |
| 16 |  | Stephanie | Yes. |
| 17 |  | R1 | And you have that many and (inaudible) |
| 18 |  | Stephanie | And the squares would be one square unit. |
| 19 |  | R1 | Okay. What about this? This is not a square. [indicates the $a \cdot b$ rectangle in the upper left corner of the model] |
| 20 |  | Stephanie | It would - [makes a noise $]$ - um so wouldn't it be there'd be $a b$ number of square units and - would each one still be one? |
| 21 |  | R1 | That's an interesting question. I want you to think about now this is $b$. [traces the line segment labeled $b$ on the upper left side of the model] the way you made the picture, do you have more of these [the $b$ 's] than you have of these [traces the a edge of the $a \cdot b$ rectangle in the upper left corner of the drawing] |

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| 22 | Stephanie | Um. No. I have more - well $a$ is larger. |
| :---: | :---: | :---: |
| 23 | R1 | $a$ is larger than $b$. Okay. |
| 24 | Stephanie | So there's more |
| 25 | R1 | Okay. But what's, if I have one of these? |
| 26 | Stephanie | Like what do you mean? Like if there's one divider? |
| 27 | R1 | Well, I have $b$ of how ma- I have $b$ of something here. |
| 28 | Stephanie | Yes. |
| 29 | R1 | What what are these things I have b of? |
| 30 | Stephanie | Units. |
| 31 | R1 | Units. And so I have a unit here. I keep going until I have $b$ of them. Right? |
| 32 | Stephanie | Yes. |
| 33 | R1 | And here, I keep going until I have $a$ of them. Right? |
| 34 | Stephanie | Yes. |
| 35 | R1 | So if you can imagine these. [marking off intervals on both sides of the $a \cdot b$ rectangle as she is speaking. Then she extends the lines to give the impression of square units.] |
| 36 | Stephanie | Um hm. |
| 37 | R1 | So what does what does the the $a b$ have to do with it? How do I get $a b$ ? |
| 38 | Stephanie | Well, that's how many units there are. |
| 39 | R1 | What does that (inaudible) |
| 40 | Stephanie | Square units there are |
| 41 | R1 | Why? |
| 42 | Stephanie | Because um [pause] Oh! Um! Because there's $a$ number of units here [along the top side of the $a \cdot b$ rectangle] |
| 43 | R1 | Um hm. |
| 44 | Stephanie | And okay. There's like if this is what it is, right? |
| 45 | R1 | Um hm. |
| 46 | Stephanie | Like if this is that piece [redraws the $a \cdot b$ rectangle on the upper left side of the paper] this is $a$ and this is $b$. [labels the longer (horizontal) side of the rectangle $A$ and the shorter (vertical) side of the rectangle $B$ ] |
| 47 | R1 | Um hm. |

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| 48 | Stephanie | There's $a$ number of units here, like this part [traces the air over the side she labeled $A$ ] |
| :---: | :---: | :---: |
| 49 | R1 | Hm. |
| 50 | Stephanie | and there's $b$ number of units here [vertically], |
| 51 | R1 | Um hm. |
| 52 | Stephanie | so if you mult and you want to get like this square. [sectioned off what looks like one square unit at the left side of the rectangle she drew] |
| 53 | R1 | Um hm. |
| 54 | Stephanie | And that's $a$ [touches the top of the square she sectioned off] times $b$ [touches the left side of the square] and there's like that many number [marks off 2 more squares by drawing vertical lines through the rectangle] and that would be $a$ times $b$, so you'd have |
| 55 | R1 | But this is not $a$. This is one and this is one. |
| 56 | Stephanie | Well, yeah, but |
| 57 | R1 | It's just that you have uh $a$ of these ones [indicates horizontally] and $b$ of these ones. [indicates vertically] |
| 58 | Stephanie | Yeah. |
| 59 | R1 | So I'm trying to understand, how do you get $a b$ ? |
| 60 | Stephanie | $a b$ what? Like? |
| 61 | R1 | As a total number of square units in that section. |
| 62 | Stephanie | In this whole |
| 63 | R1 | Yeah. |
| 64 | Stephanie | thing? |
| 65 | R1 | Yeah. [pause] Well, suppose you thought of $a$ and $b$ being particular numbers. |
| 66 | Stephanie | Um hm. |
| 67 | R1 | Suppose $a$ were five and $b$ were two. |
| 68 | Stephanie | Okay. |
| 69 | R1 | You know ahead of time |
| 70 | Stephanie | (inaudible) |
| 71 | R1 | without thinking that you're going to get |
| 72 | Stephanie | Ten. |


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| 73 |  | R1 | How many of those little squares? Ten. But I want you to <br> be able to imagine how those ten get generated when $b$ is <br> two |
| :--- | :--- | :--- | :--- |
| 74 |  | Stephanie | Um hm. |
| 75 | R1 | and $a$ is five. I want you to really in your mind to try to <br> think of how they come about. 'Cause because this is the <br> kind of power that's going to help you in mathematics as you <br> move along. Not just to say that there are $a b$. Let's not <br> worry think about that. That's a fast way to get an answer, <br> but how are they coming? That's that's the real way you're <br> going to develop this ability to do higher level mathematics. |  |

