

**A STRATEGY FOR EVALUATING THE QUALITY OF TRACE  
ALIGNMENT TOOLS BASED ON A MARKOV MODEL**

by

**XIAO BO**

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Professor Ivan Marsic

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# **ABSTRACT OF THE THESIS**

## **A STRATEGY FOR EVALUATING THE QUALITY OF TRACE ALIGNMENT**

### **TOOLS BASED ON A MARKOV MODEL**

**BY XIAO BO**

Thesis Director:

Professor Ivan Marsic

Trace alignment of event logs is used to understand and improve business processes. A key missing component of current approaches for performing trace alignment is a methodology to measure the quality of alignment. We propose a novel approach for generating random event logs that can be used for testing and evaluating trace alignment tools. We first extracted a statistical model from 437 real-world traces from Children's National Medical Center in Washington DC (CNMC). We then created a guide tree and prune it to a minimum spanning tree based on user defined trace number in output event log. The final step is to fill this tree. Each node in this tree contains a trace. Each leaf node represents a trace in output event log. The root node is filled by a user-defined sequence and each child node is mutate from parent node based on the statistical model. To validate our approach, we used a concept of replay fitness score. Replay fitness score is used to quantify the extent to which a model can reproduce the traces recorded in an event log. It's between 0 and 1. The value 1 means that the model can perfectly replay the event log and 0 means that the model cannot reply the log. Comparing with process model (Petri-Net) extracted from 437 real-world traces, the output event log of our system can constantly get a score of 0.8.

Therefore, our results are relevant not for only validation of trace alignment tools but also for other process mining tools.

## **ACKNOWLEDGEMENT AND DEDICATION**

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## CHAPTER 1 : INTRODUCTION

### 1.1 Background and Motivation

In many processes, events can be recorded in an event log in which the events within a particular process execution ( “trace” ) and their time of execution ( “timestamp” ) are recorded. The event log can then be used to determine the pattern of sequences in which a process is executed. Determining these sequences is particularly challenging for complex processes for which the steps of the process are not well-known or when real-world uncertainties introduce a large amount of variability in process execution. Mining complex event logs for execution patterns and non-standard activities, however, may be important for understanding workflow and improving process quality and productivity.

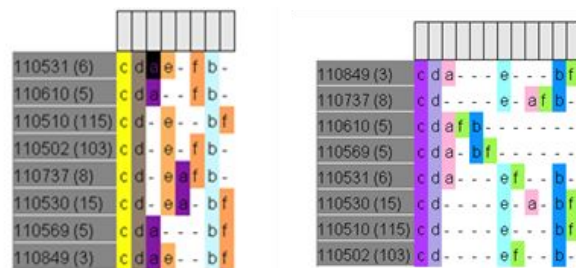
Process mining approaches have been developed for identifying successful and unsuccessful patterns of process execution and identifying deviations within these processes that may be associated with adverse events [19]. A recent process mining approach for performing this type of analysis is “trace alignment,” where the traces of events are aligned to identify the flow of events corresponding to the standard practice (known as “consensus sequence” ) [3]. Because patient-evaluation tasks during trauma resuscitation are standardized and prioritized, it appropriate to apply trace alignment on resuscitation event logs. Medical experts could use trace alignment techniques to visualize the event traces and discover the consensus sequence to understand the “average” case. Trace alignment is widely used for studying genetic

sequences and there are well-established techniques for evaluating the quality of trace alignment algorithms [22]. However, trace alignment of business process logs is new and such techniques do not yet exist. This thesis focuses on developing a quality measure for trace alignment algorithms.

Our problem domain is trauma resuscitation — the initial care of severely injured patients in the emergency department. In trauma resuscitation, the ordering of tasks for evaluating the patient is essential to appropriate identification and management of potentially life-threatening injuries. It has been observed that critically-injured patients have up to a four-fold higher risk of death from errors than general hospital patients [17], with nearly half of these preventable deaths related to errors that occur during the initial resuscitation phase of treatment [7][12]. To standardize the resuscitation process and reduce variability, trauma centers around the world have adopted a protocol (the Advanced Trauma Life Support protocol [ATLS]), which prioritizes evaluation and management tasks [9]. The key components of the first phase of ATLS (the primary survey) can be followed using the acronym “ABCDE”, represent the steps of airway evaluation (airway or “A”), evaluating respiratory mechanics (breathing or “B”), assessing and managing circulatory status (circulation of “C”), evaluating neurological status (disability of “D”) and ensuring the patient is properly exposed (exposure or “E”). Given the potential benefits of ensuring ATLS protocol compliance, our long-term goal is to build an automatic decision-support system that will help reduce human errors during trauma resuscitation.

## 1.2 Problem Statement

Trace alignment strategies have been developed for business process mining but these strategies can yield diverse results. No established methods no exist for evaluating the quality of these alignment results. As an example, an alignment of 268 ATLS traces was performed for a set of ATLS tasks using two different trace alignment strategies using a plugin in ProM 6.3<sup>1</sup> (Figure 1). Despite using the same initial data set, different results were obtained when a block-shift alignment algorithm (right of Figure 1) or regular alignment algorithm [3] that does not use block-shift alignment (left of Figure 1) was used. For example, in these two alignments the trace numbered “110531” has different length and position of gaps (“-”). These differences will also make their consensus sequence different as well. These two alignments are very different and their consensus sequence are different as well.



**Figure 1: Example trace alignments for the same event log using two different algorithms available in ProM 6.3. The left chart was produced using a regular alignment algorithm and the right chart additionally used the block shift algorithm. The letters stand for: c = airway assessment, d = breath sounds, a = palpation of central pulses, e = palpation of distal pulses, b = Glasgow Coma Score (GCS) assessment, f = pupil exam.**

<sup>1</sup> ProM 6.3 website: <http://www.promtools.org/prom6/>

Given the results of trace alignment may differ based on the method used, it is necessary to have a benchmark that can measure the quality of output of each trace alignment algorithm. We propose that this type of a benchmark should address the following two issues:

- **Generating Artificial Event Logs:** The tool should be able to generate random event logs based on the process model. During a business process execution (in our case, trauma resuscitation), the workers may not follow the standard ordering of tasks because of errors or other reasons. The tool should be able to reproduce the kind of variability present in real executions of the process.
- **Consensus Sequence Evaluation:** The tool should be able to evaluate the quality of the computed consensus sequence by comparing it with each trace in the input event log.

### **1.3 Related Work**

In the area of process mining, the main approach to creating benchmark datasets is based on a generative framework for representing well-understood processes (e.g., PLG Framework [5]). The approach is based on a context-free grammar of commonly observed patterns of event sequences, such as “sequence,” “split and merge,” or “loop”. Each production of this grammar is associated with a probability of occurrence of a pattern in the current step. This approach may be suitable for describing well-understood existing processes or newly designed processes. However, it may not be suitable for complex and poorly understood processes such as trauma resuscitation. Because process patterns and corresponding probability distributions are

unknown, the generated event log may not be a realistic representation of actual process executions.

In a related area, previous work has been developed for generating test datasets for DNA, RNA, and protein sequence alignment (e.g., ROSE [18]). This approach is based on a phylogenetic evolution tree and a substitution model (e.g., HKY85[25]) derived from known statistics of evolution process at the molecular sequence level. It also considered insert-delete (INDEL) operations and “sequence motifs” [26] which represent regions of functional importance, where mutation is less likely to happen. The knowledge of these facts is critical to simulating the evolution process. A limitation of this approach is that it mainly focuses on evolution of each position in a given sequence but overlooks the dependencies between adjacent positions. Each position is mutated independently of the adjacent positions, reflecting the nature of genetic mutations. On the other hand, in business process the next task often depends on the current task. Therefore, we need to consider the task in the current position when selecting the “mutation” for the next position (the next task).

Sequence motif is another major factor related to the first issue. In the area of computational biology, MEME (Multiple EM for Motif Elicitation) is a widely used tool for searching repeated and un-gapped sequence patterns in a set of DNA/Protein sequences[27]. It chooses each motifs by minimizing the probability of finding an equally well-conserved pattern in random sequences. This approach may be suitable

for well-understood DNA/Protein sequences. But it may not be suitable for poorly-understood and complex process traces such as ATLS traces.

Related to the second issue of consensus sequence evaluation, two main groups of string or sequence metrics can be used [16]. The first group includes the Hamming distance metric[24], which is computationally very fast and has a low memory requirement, but they may not reflect the actual similarity between two sequences. The second group includes the edit distance (based on Levenshtein distance), which can precisely measure the similarity between two sequences but these metrics are less efficient in terms of processing speed and memory requirements.

This thesis addresses the two key issues identified earlier. First, we propose a novel methodology to generate artificial event logs of the trauma resuscitation process that can serve as test event logs for trace alignment tools. Our method is based on an equivalent of evolution tree in genetics. We can think of the “ideal” execution of the resuscitation process that is prescribed by ATLS as equivalent of the “ancestor sequence” . Any variations observed in actual resuscitations can be thought of as “mutations of the ancestor sequence” The statistical parameters of our method are derived from real resuscitations logs. Second, we propose a methodology to measure the quality of consensus sequence based on Phred-quality score [10] and edit distance[23].

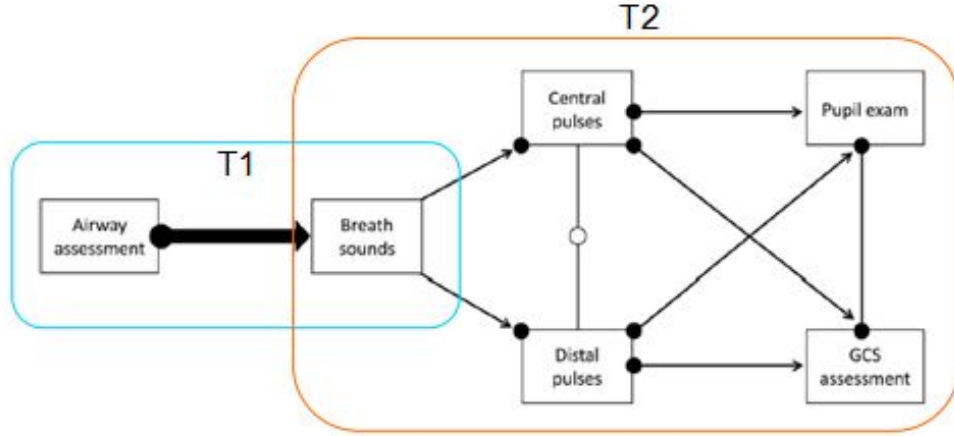
## CHAPTER 2 : PROCESS MODEL AND DATA SOURCE

### 2.1 Data Source

Our input event log is generated from video recordings at the trauma center of the Children's National Medical Center (CNMC) in Washington, DC. The data were collected over from events that occurred over eight months. The resulting log contains ATLS event traces from 437 trauma resuscitations as well as a timestamp allowing assessment of the order of event performance [8]. The approach that was used for obtaining this event log has been previously described [13][14].

### 2.2 Declarative Model and Statistical Model

A declarative model of the process for which the traces were collected was developed by medical experts based on the knowledge of the ATLS process [2] performed by the bedside evaluator (Figure 2). It included six primary ATLS survey tasks. This model represents the best practice for ordering and inclusion of these tasks. For example, “breath sounds” should not happen before “airway assessment” is accomplished and “GCS assessment” should not occur unless either the “central pulse” or “distal pulses” are measured. Although this is a best-practice model, actual process execution may not follow this model. First, the provider may go back to previous steps to reevaluate an observed change. Second, the process may be performed out of order because of situational variables such as the availability of needed evaluation tools or personnel.



**Figure 2: Declarative model of six key tasks of the ATLS primary survey.**

We can state the above description in a more formal way by representing a real-world business process using a first-order Markov model. Given a trace with  $M$  events, the  $i$ th event ( $1 \leq i \leq M$ ) depends on the  $(i-1)$ st event, for  $i > 1$ . The parameters of the proposed model are as follows:

- Event frequencies  $\text{PREFIX\_FREQ}(f_1, f_2, \dots, f_n)$  satisfying  $\sum_{i=1}^n f_i = 1$  are used for creating the first event in a trace.
- Mutation matrix  $T1$  represents the transition probability from the first to the second event.
- Mutation matrix  $T2$  represents the transition probability from event  $i$  to event  $i+1$ .
- Length frequencies  $L(\ell E_1, \ell E_2, \dots, \ell E_n)$ , represent the possible lengths of traces that start with different events  $E_1, E_2, \dots, E_n$ . Given a first event of type  $E_i$  in a trace, different possible lengths  $k$  of the trace occur with different frequencies  $f_k$ . Therefore,  $\ell E_i(f_1, f_2, \dots, f_n)$  represents the probability distribution of different trace lengths, given the first event =  $E_i$  and the distribution satisfies  $\sum_{k=1}^n f_k = 1$ . Let us assume that



an event trace could start with these first events:  $E1 = \text{“airway assessment”}$  or  $E2 = \text{“breath sounds.”}$  Then we need to specify  $L = \{\ell \text{ airway-assessment}, \ell \text{ breath-bounds}\}$ . For example, traces that start with “airway assessment” and be up to five events long, but only trace lengths 2 and 5 occur, and they occur equally likely. Then, the probability distribution for  $\ell \text{ airway-assessment} = \{f_1 = 0, f_2 = 0.5, f_3 = 0, f_4 = 0, f_5 = 0.5\}$ .

The model parameters (PREFIX\_FREQ, T1, T2, L) are extracted from a given event log as follows:

**Function** get\_prefix\_freq(log) **return** PREFIX\_FREQ:

PREFIX\_FREQ = {} // PREFIX\_FREQ is a Python-like

// dictionary. It could also be implemented by a hash-table.

Counter = 0

**For** trace **in** log:

First\_event = trace[0]

**If** first\_event **not in** PREFIX\_FREQ:

PREFIX\_FREQ[first\_event] = 0

**End if**

PREFIX\_FREQ[first\_event]++

Counter++

**End for**

**For** event **in** PREFIX\_FREQ:

$$\text{PREFIX\_FREQ}[\text{event}] = \text{PREFIX\_FREQ}[\text{event}] / \text{Counter}$$

**End for**

**Return** PREFIX\_FREQ

Other parameters of the model are extracted similarly. Table 1 and Table 2 show the extracted contents of T1 and T2. The letter encoding is as defined in Figure 1.

<div> <div> NEXT </div> <div> PREVIOUS </div> </div>	c	d	a	e	b	f
c	0	0.01	0.06	0.52	0.16	0.16
d	0.003	0	0.09	0.79	0.07	0.05
a	0.02	0.04	0	0.18	0.41	0.43
e	0.04	0.002	0.1	0	0.41	0.43
b	0.004	0.03	0.05	0.07	0	0.85
f	0.02	0	0.07	0.06	0.85	0

**Table 2: Contents of T2, where the letter codes are as defined in Figure 1. T2[c,d]**

**means the probability of  $i_{th}$  event = “d=breath sounds” if  $(i-1)_{th}$  event**

**“c=airway assessment,” where  $1 < i < \text{trace-length}$ .**

PREVIOUS \ NEXT	c	d	a	e	b	f
c	0	0.95	0.01	0.02	0.02	0
d	0.6	0	0.03	0.3	0.03	0.03
a	0	0	0	0	0	0
e	0	0	0	0	0	0
b	0.7	0.3	0	0	0	0
f	1	0	0	0	0	0

**Table 1: Contents of T1, where the letter codes are as defined in Figure 1. T1[c,d] means the probability of position 1 being “d=breath sounds” if position 0 was “c=airway assessment.”**

The motivation to partition the mutation matrix into T1 and T2 is to avoid the possibility that noise present in T2 affects T1. For example, based on the declarative model (Figure 2), “pupil exam” and “GCS assessment” are not acceptable in the first two steps, but are highly coupled. Based on the event log of 437 observed traces, their mutual transition probabilities after the first two steps ( “pupil exam ( GCS assessment” and “GCS assessment ( pupil exam” ) are (0.85. However, some real traces started with “pupil exam” (not adhering to the model in Figure 2), which was invariably followed by “airway assessment” (see that  $T1[f, c] = 1$  in Table 1). In such cases, if we combined all transition probabilities into a single mutation matrix, the system could generate a trace like “pupil exam ( GCS assessment ( pupil exam ( GCS assessment” , which is unacceptable because no such traces were observed. In other words, statistics from the “normal” cases (represented by the model) could distort the transition probabilities.

### 2.3 Sequence Motif Mining

In the area of process mining, sequence motif is considered as common patterns of invocations of activities in traces[28]. It's key to reflect the real execution of process model. Currently, several patterns are defined in [28]. In this paper, we utilize maximal repeats as an example. The followings are its definition[28][29]:

**Definition 1 (Maximal Repeat).** *A maximal pair in a sequence,  $s$ , is a pair of identical sub-sequences  $\alpha$  and  $\beta$  such that the symbol to the immediate left (right) of  $\alpha$  is different from the symbol to the immediate left (right) of  $\beta$ . In other words, extending  $\alpha$  and  $\beta$  on either side would destroy the equality of the two strings. A maximal pair is denoted by the triple  $(i, j, \alpha)$  where  $i$  and  $j$  correspond to the starting positions of  $\alpha$  and  $\beta$  in  $s$  with  $i \neq j$ . A maximal repeat in a sequence,  $s$ , is defined as a subsequence  $\alpha$  that occurs in a maximal pair in  $s$ .*

It captures the common sequence of activities among traces and might be evidence of common functionality[29]. It can be efficiently mined by suffix tree within linear time[30][31].

We also introduced the concept of Conservedness to measure the confidentiality of each motif. It measures the degree to which the individual activities involved in the pattern alphabet manifest as the patterns defined by the alphabet[29]. The followings are its definition[29]:

$$\text{Conservedness} = \frac{\text{NOAC}}{\mu} * (1 - \frac{\alpha}{\mu}) * 100\%, \text{ where NOAC is Non-Overlapping}$$

Alphabet Count,  $\mu$  and  $\alpha$  are the mean and standard deviation of frequencies of activities.

In actuality, we used “Pattern Abstraction” plugin to calculate sequence motifs set  $M$  from 437 actual traces. When calculating NOAC, we prefer shorter patterns. All duplicate traces are also ignored. All patterns whose length  $\leq 1$  or conserved-ness score is less than 50% are also pruned. Table 3 are discovered sequence motifs and their conserved-ness score:

Pattern Alphabet	Pattern Sequence Set	Conservedness Score
airwaydo, breathso	airwaydo->breathso	62%
	breathso->airwaydo	62%
gcsdone, pupilsdo	gcsdone->pupilsdo	61%
	pupilsdo->gcsdone	61%

**Table 3: Contents of  $M$ , where “Pattern Sequence Set” Column represents each discovered sequence motifs.**

## CHAPTER 3 : ALGORITHM

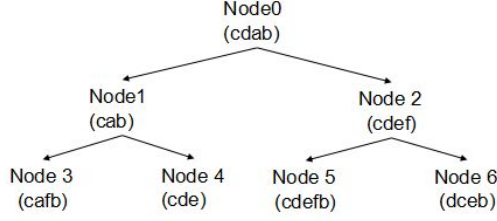
### 3.1 Overview

Our system consists of two components:

1. Trace Generator creates a random event log used in trace alignment
2. Consensus Evaluator evaluates the generated consensus sequence.

### 3.2 Trace Generator

The trace generator produces a random event log simulating real-world variability of the business process. It is common to represent this process by a guide tree, where each node contains a trace (Figure 3). The root node (Node 0) contains an “ideal” trace of standard ordering of tasks, and the other nodes contain variations. When executing the process in a standard way, errors may occur in the actual execution would “mutate” from Node 0 to Node 1. For instance, suppose the trace in Node 0 is “airway assessment -> breath sounds -> central pulse -> GCS assessment”. “Breath sounds” may have been skipped in the trace in Node 1 and Node 1 become “airway assessment -> central pulse -> GCS assessment”. As more mistakes occur, the actual execution may further “mutate” from Node 1 to Node 4.



**Figure 3: An example guide tree used for simulating real-world variability of trauma resuscitation. The letter encoding for example traces in the parentheses is as defined in Figure 1.**

In addition to (PREFIX\_FREQ, T1, T2, L, M ), the generator requires the following input:

- An Ancestor Trace S: This trace is the standard trace used to generate variations. This trace should be user-defined. If the user does provide the standard trace (e.g., because of a poorly specified process), a random trace of length  $\ell$  will be generated based on the model parameters (PREFIX\_FREQ, T1, T2 and L).
- Edge Distance D: This number represents the frequencies of mutation from parent node to its children nodes. In Figure 3, if  $D = 8$  Node 1 mutates eight times before reaching Node 4. The edge distance is used to create a mutation guide tree which acts as a mapping for generating a random event log [18].
- Revival Probability R: This number represents the probability to generate a child trace without considering the parent trace. For instance, Node 4 may be created as a

random trace rather than a mutation of Node 1. The main motivation for this feature is to increase the randomness of output datasets.

- Trace Number N: This number determines the number of traces in the output event log E (defined below).

- Tree Depth d: This number represents the depth of the guide tree, i.e., how many generations the tree will evolve away from the root trace. For example, in Figure 3,  $d = 2$ .

The output of the trace generator is:

- Event Log E: The event log contains all random traces that are generated by the trace generator.

The following is the pseudocode of the algorithm:

**Function** trace\_generator(S, D, d, N, R, PREFIX\_FREQ, T1, T2, L, M) **return** E

**If** S is undefined

S = create\_sub\_trace(null, 0, n, PREFIX\_FREQ, T1, T2, L)

**End if**

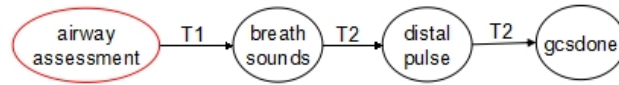
T = create\_guide\_tree(D, d)

prune\_tree(T, N)

T.root = S



```
fill_tree(T.root, M)
```



**Figure 4: Generation of a sample sub trace.**

**In this case, seed event  $E$  = airway assessment, start position  $P = 0$ , and trace length  $\ell = 4$ .**

```
Traces = get_traces(T)
```

**Return Traces**

Function `fill_tree()` is implemented as a recursion:

**Function** `fill_tree(T.root, M)`

**For** children of `T.root` do

`Children.seq = mutate(T.root)`

`Define_motif_positions(Children, M)`

`fill_tree(Children)`

**End for**

The remaining functions are defined in the following subsections.

### 3.2.1 Generating the Sub Traces

The function `create_sub_trace(E, P,  $\ell$ , PREFIX_FREQ, T1, T2, L)` is the core function for generating event logs. It returns a trace of length  $\ell$ . In addition to `(PREFIX_FREQ, T1, T2, L)`, it also requires the following inputs:

- **Seed Event E:** The first event in the trace or sub-trace that will be generated.

- Start Position  $P$ : The position of the seed event in the original trace. This number will determines what the transition model ( $T1$ ,  $T2$ ) will be used for generating a sub-trace.
- Trace Length  $\ell$ : The length of the target (output) sub-trace.

Figure 4 shows an example creation of a sub-trace. Because the seed event is also the first event in the parent-node trace, the second event in a sub-trace is determined by  $E$  and  $T1$  based on the model (Figure 2). The third event is based on  $T2$  and the second event, and so is the fourth event. If the input seed event is null, the seed event will be generated from `PREFIX_FREQ`.

### 3.2.2 Generating the Mutation Guide Tree

Creation of the mutation guide tree is done in the function `create_guide_tree()`. After the tree is created,  $N$  nodes are randomly marked as “selected,” because the user requested  $N$  traces in the output event log  $E$ . To reduce the computational complexity, we compute the minimum spanning tree and prune the tree. For example, in Figure 3, when Nodes 3 and 4 are selected, Nodes 2, 5, and 6 will be removed because they are not relevant to reaching Nodes 3 and 4 from the root node. After the minimum spanning tree is generated, the system generates the output event log  $E$  from the root node by `fill_tree()` and `get_traces()`.

### 3.2.3 Generating Children Traces

The core function for children trace creation is the function `mutate()`. The followings are its main steps:

1. Generate trace of length  $\ell$  based on the type  $E_i$  of the first event in the trace:

$$\ell = \text{getLength}(E_i, L)$$

2. Determine the mutation start position STARTPOS ( $0 \leq \text{STARTPOS} < \ell$ )

3. Create sub-trace based on  $T_{\text{old}}[\text{STARTPOS}]$ :

$$T_{\text{sub}} = \text{create\_sub\_trace}(T_{\text{old}}[\text{STARTPOS}], \text{STARTPOS}, \\ \ell - \text{STARTPOS}, \text{PREFIX\_FREQ}, T1, T2, L)$$

4. Create child trace by removing the old sub-trace starting at position STARTPOS and appending instead it the created sub-trace:

$$T_{\text{old}}.\text{RemoveAll}(\text{STARTPOS}, T_{\text{old}}.\text{length}); \\ T_{\text{new}} = T_{\text{old}}.\text{append}(T_{\text{sub}})$$

By above steps, the INDEL operations are realized since L contains all possible trace lengths. The sequence motif information is also represented in T1, T2. These steps are repeated for edge distance D times in order to maintain the randomness of child traces.

### 3.2.4 Creation of Sequence Motif

Creation of sequence motif is implemented by `define_motif_positions()`. When defining sequence motifs in children trace, we search each pattern in M and mark

corresponding positions as “important”. These “important” positions will determines the penalty score in consensus sequence evaluation.

### 3.3 Consensus Sequence Evaluator

The quality of consensus sequence is evaluated from two aspects: confidence about the element in each position and similarity between traces in event log and consensus sequence. Phred-quality score is used to measure the confidence for each position:

$$Q = -10 \cdot \log_{10}(P), \text{ where } Q \text{ represents Phread-quality score and } P \text{ represents base-calling error probability [10][11].}$$

Q, however, only estimates the confidence of the element in each position in the consensus sequence, independently of other positions. For this reason, we use regular edit distance to measure similarity between the consensus sequence and individual traces in test event logs instead of Q. “Sequence motifs” which represent critical positions in the root trace that are subject to lower mutation rates compared to other positions. Therefore, we add a “penalty” in the quality score formula, to penalize mutations in the corresponding positions. The followings are formula to compare consensus sequence and each trace:

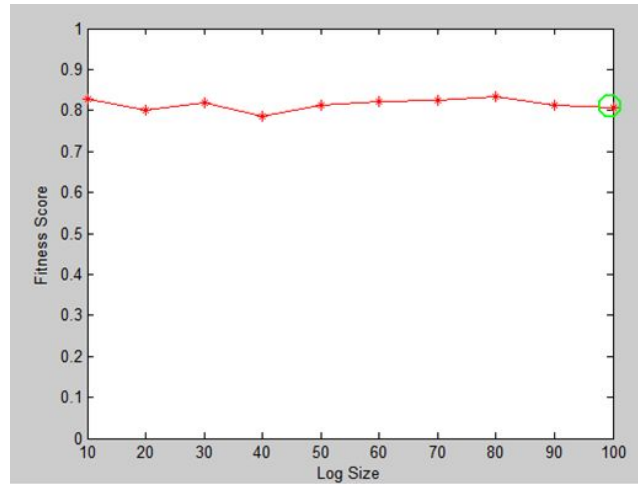
$$Q_2 = \text{Edit\_Distance} + X * N_{dif}, \text{ where } X \text{ is a user-defined coefficient and } N_{dif} \text{ represents number of mutated critical positions contains in consensus sequence.}$$

## CHAPTER 4 : RESULTS AND DISCUSSION

To test our trace generator, we used the concept of Replay Fitness Score [4][19]. This score is used to quantify the extent to which a model can reproduce the traces recorded in an event log. The score is computed as [4]:

$$Q_{rf} = 1 - \frac{\text{cost for aligning model and event log}}{\text{Minimal cost to align arbitrary event log on model and vice versa}}$$

where  $Q_{rf}$  is between 0 and 1. The value 1 means that the model can perfectly replay the event log and 0 means that the model cannot reply the log.



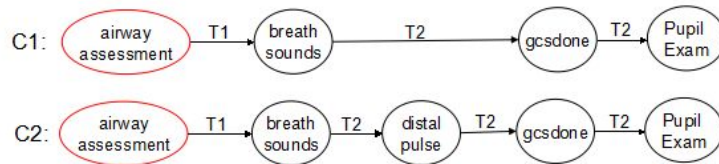
**Figure 5: Replay Fitness Score of artificial event logs generated by our tool, compared to the Petri-net model created by ProM from 437 actual event traces.**

To explore the properties of our trace generator, we generated 10 event logs with 10 to 100 traces each. The ancestor trace  $S$  is “airway assessment -> breath sounds -> pupil exam -> GCS assessment -> pupil exam -> GCS assessment” and the guide tree is created with the parameters  $d = 10$ ,  $D = 1$  and  $R = 0.5$  (Section 3.2). We also computed an approximate model (Petri Net) of 437 traces by using the ProM plugin named “Mine a Petri net using ILP” [21]. Next, we computed the fitness score using

the ProM plugin named “Replay a log on Petri Net for conformance checking.” The fitness score determines how well our artificially generated event log fits the Petri Net model of the actual event log [1][20]. The core algorithm is a cost-based A\* algorithm [1]. The fitness score Qrf for our event log generator is around 0.8 (Figure 5). Based on the definition of Qrf, it should be equal to 1 for all artificial event logs that perfectly simulate the real-world process execution. A potential reason that event logs generated by our tool generally have lower fitness score (Figure 5) is that the Integer Linear Programming (ILP) approach performs well in terms of speed but lacks in precision [21].

To further understand the characteristics of our trace generator, we used one of event logs from Figure 5. This event log had 100 artificial traces and its fitness score is circled by green in Figure 5. We computed its consensus sequence C1 using the trace alignment plugin of ProM as  $C1 = \text{“airway assessment} \rightarrow \text{breath sounds} \rightarrow \text{GCS assessment} \rightarrow \text{pupil exam.”}$  The plugin uses the Euclidean distance [8] as part of the alignment process. We also computed the consensus sequence C2 of the 437 actual traces using same algorithm and obtained  $C2 = \text{“airway assessment} \rightarrow \text{breath sounds} \rightarrow \text{distal pulse} \rightarrow \text{GCS assessment} \rightarrow \text{Pupil Exam.”}$  When these two consensus sequences are compared, the only difference is that in C2 “distal pulse” is missing (Figure 6). Based on T2 (Table 2), both “GCS assessment” and “distal pulse” can follow after a “breath sounds” event, but the probability  $T2[\text{breath sounds, distal pulse}]$  is much greater than  $T2[\text{breath sounds, GCS assessment}]$ .

Therefore, the consensus sequence C1 of our artificial event log should not have omitted “distal pulse” if our tool perfectly simulated the real-world process execution. There are two potential explanations for this shortcoming. First, the trace alignment algorithm in ProM [3] may not be robust enough to handle some real-world variability of event traces. Second, 100 traces in our artificial event log or 437 actual traces may be insufficient for accurate representation of statistical properties of the trauma resuscitation process.



**Figure 6: Comparison of the consensus sequence for an artificially-generated event log (C1) to that of the 437 actual event traces of trauma resuscitation (C2).**

We used Phred-quality score for consensus sequence evaluation, which has proved to provide a robust metric for evaluating the performance of alignment tools for genetic sequences [10][11]. Phred-quality score to measure the confidence about each position in a consensus sequence. However, since our problem domain is different, this issue needs further exploration.

## CHAPTER 5 : CONCLUSION AND FUTURE WORK

The event logs created by our methodology are artificial datasets used for evaluating how the ProM trace alignment tool performs on a given event log. Our experimental results showed that our tool can generate random event logs that can replay the real execution of a declarative model of ATLS. Our tool combines the strengths of several existing evaluation frameworks (e.g., PLG and ROSE), such as using guide tree and process model to generate realistic event logs of the trauma resuscitation process. Unlike PLG, we use the statistical model extracted from real data and a guide tree to event traces. Unlike Rose, which mutates each position in the sequence independently of its neighbors, we consider the current task when generating the next task. In this sense, our tool “grows” the event traces from starting event to the final event. Furthermore, we extracted sequence motifs from real data and defines the positions of functional importance. For these reasons, our tool is suitable for evaluating trace alignment tools for their potential use for studying event logs of trauma resuscitations.

Our model was designed to simulate the event traces resulting from real execution of an ATLS-based process. We plan to improve this evaluation tool in several ways. First, the model for INDEL operation is unrealistically simple. Currently, we randomly choose a position in the trace and then grow a new sub-trace from it. However, not all positions have the same probability that a mutation will occur. For instance, about 78% of our dataset of 437 traces started with “airway assessment”, and about 95% of those traces which started with “airway assessment” had “breath sounds” in the



second position. Second, as discussed in Section 4, we need to prove whether Phred-Quality Score is accurate for consensus sequence evaluation. Third, some combinations of tasks are critical and are less likely to vary (i.e., mutate), because the workers are trained to pay special attention to these tasks. However, statistical commonly sequence pattern may not contains all of these information. To address this potential finding, we also plan to introduce domain-knowledge and define “motifs,” and suppress mutation on these tasks.

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## APPENDIX A : ALGORITHM TO EXTRACT STATISTICAL MODEL

### 1. Algorithm To Extract PREFIX\_FREQ:

**Function** GET\_PREFIX\_FREQ(Event-Log) **return** PREFIX\_FREQ:

PREFIX\_FREQ = {}      // PREFIX is a dictionary

COUNTER = 0

**For** trace **in** Event-Log:

    Event = trace[0]

**If** Event **not in** PREFIX\_FREQ:

        PREFIX\_FREQ[Event] = 0

**End If**

    PREFIX\_FREQ[Event]++

    COUNTER++

**End for**

**For** event **in** PREFIX\_FREQ:

    PREFIX\_FREQ[event] = PREFIX\_FREQ[event]/COUNTER

**End For**

**Return** PREFIX\_FREQ

### 2. Algorithm To Extract T1:

**Function** GET\_T1(Event-Log) **return** T1:

T1 = {}      // T1 is a dictionary

**For** trace **in** Event-Log:

**If** trace.length < 2:

**Continue**

First\_Event = trace[0]

Second\_Event = trace[1]

**If** First\_Event **not in** T1:

T1[First\_Event] = {}

**End if**

**If** Second\_Event **not in** T1[First\_Event]:

T1[First\_Event][Second\_Event] = 0

**End if**

T1[First\_Event][Second\_Event]++

**End For**

**For** first\_event **in** T1:

COUNTER = 0

**For** second\_event **in** T1[first\_event]:

COUNTER = COUNTER + T1[first\_event][second\_event]

**End for**

**For** second\_event **in** T1[first\_event]:

T1[first\_event][second\_event] = T1[first\_event][second\_event]/COUNTER

**End for**

**Return** T1

### 3. Algorithm To Extract T2:

**Function** GET\_T2(log) **return** T2:

T2 = {}

**For** trace **in** log:

**If** trace.length <= 2:

        Continue

**End if**

**For** i **in** range(1,trace.length-1):

        Current\_Event = trace[i]

        Next\_Event = trace[i+1]

**If** Current\_Event **not in** T2:

            T2[Current\_Event] = {}

**End if**

**If** Next\_Event **not in** T2[Current\_Event]:

            T2[Current\_Event][Next\_Event] = 0

**End if**

        T2[Current\_Event][Next\_Event]++

**End for**

**For** Current\_Event **in** T2:

    COUNTER = 0

**For** Next\_Event **in** T2[Current\_Event]:

        COUNTER = COUNTER + T2[Current\_Event][Next\_Event]

**End for**

**For** Next\_Event **in** T2[Current\_Event]:

$T2[Current\_Event][Next\_Event] = T2[Current\_Event][Next\_Event] / Counter$

**End for**

**Return** T2

#### **4. Algorithm To Extract L:**

**Function** GET\_L(Event-Log) **return** PREFIX\_FREQ:

L = {}      // L is a Python-like dictionary

**For** trace **in** Event-Log:

    First\_Event = trace[0]

    Cur\_Len = trace.length

**If** First\_Event **not in** L:

        L[First\_Event] = {}

**End If**

**If** Cur\_Len **not in** L[First\_Event]:

        L[First\_Event][Cur\_Len] = 0

**End If**

    L[First\_Event][Cur\_Len]++

**End for**

**For** event **in** L:

    Counter = 0

**For** Cur\_Len **in** L[event]:

        Counter = Counter + L[event][Cur\_Len]

**End for**



**For** Cur\_Len **in** L[event]:

L[event][Cur\_Len] = L[event][Cur\_Len] / Counter

**End for**

**End For**

**Return** L

## APPENDIX B : ALGORITHM TO GENERATE CHILDREN TRACE (JAVA CODE)

```

public String[] mutate(String[] oldTrace) {

    ArrayList<String> buffer = new ArrayList<String>(

        Arrays.asList(oldTrace));

    Random dice = new Random();

    HashMap<String, Float> subDict = new HashMap<String, Float>();

    for (int i = 0; i < this.distance; i++) {

        if (dice.nextFloat() >= this.revivalProb) {

            String firstEvent = this.getEvent(this.PREFIX_FREQ);

            int length = this.getLength(firstEvent);

            buffer = this.createSubTrace(firstEvent, 0, length);

            continue;

        }

        int length = this.getLength(oldTrace[0]);

        int curLen = buffer.size();

        int startPos = 0;

        if (length >= curLen) {

            startPos = dice.nextInt(curLen);

        } else {

            startPos = dice.nextInt(length);

        }
    }
}

```

```

// System.out.println(length+" "+startPos);

ArrayList<String> subTrace = this.createSubTrace(
    buffer.get(startPos), startPos, length - startPos);

buffer = new ArrayList<String>(buffer.subList(0, startPos));

if (subTrace != null) {
    buffer.addAll(subTrace);
}

}

return buffer.toArray(new String[buffer.size()]);
}

```

```

private int getLength(String event) {

    HashMap<String, Float> subDict = this.L.get(event);

    Random dice = new Random();

    float counter = 0, prob = dice.nextFloat();

    String length = "0";

    for (String key : subDict.keySet()) {

        counter = counter + subDict.get(key);

        if (counter >= prob) {

            length = key;

            break;
        }
    }
}

```

```

    }

    return Integer.valueOf(length);
}

private ArrayList<String> createSubTrace(String seed, int startPos,

    int length) {

    HashMap<String, Float> subDict = null;

    String[] subTrace = new String[length];

    if (seed == null) {

        subDict = this.PREFIX_FREQ;

        seed = this.getEvent(subDict);

    }

    if (length == 0) {

        return null;

    }

    subTrace[0] = seed;

    // System.out.println(startPos);

    for (int i = startPos + 1; i < startPos + length; i++) {

        int realIndex = i - startPos - 1;

        String prevEvent = subTrace[realIndex];

        subDict = this.T2.get(prevEvent);

        if (i == 1) {

```

```

        subDict = this.T1.get(prevEvent);

    }

    // System.out.println(startPos+" "+(startPos+length));

    // System.out.println(prevEvent);

    String curEvent = this.getEvent(subDict);

    subTrace[realIndex + 1] = curEvent;

}

return new ArrayList<String>(Arrays.asList(subTrace));

}

public String getEvent(HashMap<String, Float> subDict) {

    Random dice = new Random();

    float sum = 0, prob = dice.nextFloat();

    String newEvent = null;

    for (String event : subDict.keySet()) {

        sum = sum + subDict.get(event);

        if (sum > prob) {

            newEvent = event;

            break;

        }

    }

    return newEvent;

}

```

## APPENDIX C : ALGORITHM FOR COMPUTING MINIMUM SPANNING TREE (JAVA CODE)

```

public void pruneTree() {
    ArrayList<TreeNode> nodeList = this.getNodeList();
    Random dice = new Random();
    int counter = 0;
    while (counter < this.nodeNum) {
        int selectIndex = dice.nextInt(nodeList.size());
        TreeNode cur = nodeList.get(selectIndex);
        if (!cur.selected) {
            cur.selected = true;
            cur.relevant = true;
            counter++;
        }
    }
    this.root.relevant = true;
    for (int i = 0; i < nodeList.size(); i++) {
        TreeNode cur = nodeList.get(i);
        if (cur.selected) {
            while (cur != this.root) {
                cur.father.relevant = true;
                cur = cur.father;
            }
        }
    }
    this.compressTree(this.root);
}

private void compressTree(TreeNode cur) {
    if (cur == null) {
        return;
    }
    if (cur.leftChild != null) {
        if (!cur.leftChild.relevant) {
            cur.leftChild = null;
        } else {
            this.compressTree(cur.leftChild);
        }
    }
    if (cur.rightChild != null) {
        if (!cur.rightChild.relevant) {
            cur.rightChild = null;
        } else {

```

```
        this.compressTree(cur.rightChild);  
    }  
}  
}
```

## APPENDIX D: ALGORITHM FOR FILLING THE GUIDE TREE

```

public void fillTree() {

    this.root.trace = this.ANCESTOR;

    this.defineMotifs(this.root);

    this.fillNodes(this.root);

}

public void defineMotifs(TreeNode t) {

    if (t == null) {

        return;

    }

    HashSet<Integer> positions = new HashSet<Integer>();

    for(String[] motif : this.MOTIFS.keySet()){

        String str = this.string2character(t.trace);

        String subStr = this.string2character(motif);

        int index = str.indexOf(subStr);

        System.out.println(index);

        while(index>=0){

            for(int i=0;i<subStr.length();i++){

                positions.add(index+i);

            }

            index = str.indexOf(str, index + 1);

```



```

        }

    }

    t.motifs = positions.toArray(new Integer[positions.size()]);

    Arrays.sort(t.motifs);
}

```

```

private String string2character(String[] trace){

    StringBuilder str = new StringBuilder();

    for(String event : trace){

        str.append(event.charAt(0));

    }

    return str.toString();

}

```

```

private void fillNodes(TreeNode father) {

    if (father == null) {

        return;

    }

    if (father.leftChild != null) {

        father.leftChild.trace = this.mutate(father.trace);

        this.defineMotifs(father.leftChild);

        this.fillNodes(father.leftChild);

    }

}

```

```
}  
  
if (father.rightChild != null) {  
  
    father.rightChild.trace = this.mutate(father.trace);  
  
    this.defineMotifs(father.rightChild);  
  
    this.fillNodes(father.rightChild);  
  
}  
  
}
```