

<b>Description: Building Large Models to Show Equivalence: An Exploration (classroom view)</b> <b>Date: 1993-10-07</b> <b>Location: Colts Neck Elementary School</b> <b>Researcher: Professor Carolyn Maher</b>	<b>Transcriber(s): Yankelewitz, Dina</b> <b>Verifier(s): Yedman, Madeline</b> <b>Date Transcribed: Spring 2009</b> <b>Page: 1 of 24</b>
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- 9.2.1 5:33 T/R 1: Well, good morning! [students answer good morning]. I saw how hard you were working yesterday, I looked at tapes last night and early this morning, and I feel, uh, very close to you. You had breakfast with me this morning some of you, and you had, um, I guess, some dinner with me and one of my colleagues who was visiting, and it was really wonderful to watch the way you were solving those problems. Um, and I read your papers, so did Dr. Martino, and uh, I was so impressed at how hard you were all working and the wonderful wonderful thinking that you shared with me in the pictures you drew and the models you made. Yesterday I was working with a group of thirty teachers - that's why I couldn't be here - um, Mr. Purdy was there in the afternoon, he was here in the morning, and I was showing them some of your work and weren't they impressed?
- 9.2.2 Purdy: They were very impressed.
- 9.2.3 T/R 1: They were very impressed, and your teacher Mrs. Phillips knows some of these other teachers and they said "Oh my goodness, those students are doing such wonderful mathematics!" They were so pleased. So I'm glad to be here, today, I need to tell you, I'm going to be gone for a couple of weeks, um, we have to go to a conference in California, Dr. Martino and I, and uh, we're leaving next week. Dr. Martino will be here Monday, and then it will be two weeks before we come back. Um, so while we're gone, and the other mathematics you're doing with Mrs. Phillips, I hope you'll continue to write to me about what you're doing and to Dr. Martino, so, we sort of can still feel close to what's going on when we're not here. So would you do that [Students nod and say Mmm hmmm]? Would you be writing [CT says "Sure"] and then I, we won't be able to wait until we come back. Um, and then we'll be here for a little while again. Ok? Um, I was watching and reading and I was really interested in some of the questions that you were sort of thinking about as you were making your models and I noticed that everyone made a few models in the problems you were solving, isn't that right? You all were making a few models and I know I know Erik was making a model and he's worried about how he can get it on his paper, right? And, cuz it was a large one on his desk, and I'm kind of thinking, um, how are they

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gonna get it one the overhead when they share it with us, right? That's gonna be a problem. But I thought, you know, we can always get a couple of pieces of paper and tape them together if you had to, that's ok. You know, you can fold them or something. So, we'll figure out ways to record even if some of your models do get bigger. Um, what I was going to ask you to think about, um, one of the problems a little bit before we even shared and that was the problem that I think everyone did work on, uh, the second one, which was larger, three quarters or [students say two thirds] two thirds. Did everyone here work on that problem? Somebody might have been ab- raise your hand if you worked on that problem. [All students shown raise their hands] Which is larger, three quarters or two thirds? Ok, and how many of you built more than one model to show a solutions to that problem? [a few students raise their hands]. How many of you built three models? [No hands are raised] Some of you built two models, were working on two models? Yes, I'm really interested in this. Um, do you remember anything about the problem? I know you don't have the rods yet, but I want you to try to imagine in your mind if you can remember what you did when you solved the problem, which is larger three quarters or two thirds? By the way, do you remember which was larger? [students say mmm hmm] You do remember [mmm hmmm, yeah]. How many of you remember which is larger? [some students raise their hands] Can you think about it in your minds, what you built? I'm kind of curious, what helps you remember, Sarah?

- 9.2.4 9:36 Sarah: Uh, that two thirds is larger
- 9.2.5 T/R 1: She remembers that two thirds is larger. [Erik:I remember something] Erik?
- 9.2.6 Erik: I remember that two, wait, three fourths is larger than two thirds by one twelfth or two twenty-fourths.
- 9.2.7 T/R 1: Erik remembers it differently. Anybody else? Anybody else remember it? You're not so sure? Michael, what do you remember?
- 9.2.8 Michael: I agree with Erik, um, because, that's, I remember three fourths being bigger than it because the four, wait I had three light greens and then only two purples and the three light greens were larger.

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- 9.2.9 T/R 1: Hmm, it could be we need our rods. It's hard for me to remember these. You think that will help? [students say yes].  
Ok. Could you give out these for me, Jackie to the tables?  
What are you thinking, Meredith, while we're giving these -  
Erik [inaudible] Alan. [Students distributes sets of Cuisenaire rods]. Meredith?
- 9.2.10 11:36 Erik: Ok, what do we need?  
9.2.11 Alan: We need the uh, two oranges and the purple  
9.2.12 Erik: Yeah, I remember, two oranges and the purple. This was our last one, because I remember I was tracing on it,  
9.2.13 Alan: Oh, yeah,  
9.2.14 Erik: Two oranges, one purple, the browns I remember were the thirds.  
9.2.15 Alan: Yeah. And the halves were the  
9.2.16 Erik: We didn't need, we didn't need halves, remember?  
9.2.17 Alan: I know, but we did build em.  
9.2.18 Erik: I think it was the blacks, or the dark greens.  
9.2.19 12:08 Alan: Dark greens fourthed it.  
9.2.20 Erik: Yeah,  
9.2.21 CT: [hands out mats] Put the mats under because it's far too noisy  
9.2.22 Alan: Yeah, Erik, have a mat, it's too noisy. Have a mat.  
9.2.23 Erik: Ok, one purple, brown,  
9.2.24 Alan: Yeah, try the purple, the dark greens did fourth it.  
9.2.25 Erik: They did, I know.  
9.2.26 Alan: Yeah. And then the twenty-  
9.2.27 Erik: No, twelfths were the reds.  
9.2.28 Alan: Twelfths were the reds, and then the whites were the twenty-fourths.  
9.2.29 Erik: Oh, they're copying us, they're doing twenty-fourths!  
9.2.30 Alan: Hey! Somebody's copying.  
9.2.31 Erik: Oh crap, we don't have any more reds! Seven we have eight nine ten, we just need two more  
9.2.32 Alan: [To group of three] Can you spare two red rods? Can we have some? Here we go!  
9.2.33 Erik: Two three four five six.  
9.2.34 Alan: Do you have twenty-four twenty-fourths?  
9.2.35 Erik: Probably not.  
9.2.36 Alan: Oh, I think you overdid it, you overdid it,  
9.2.37 Erik: What?  
9.2.38 Alan: Well, maybe not.  
9.2.39 Erik: What do you mean, overdid it?

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- 9.2.40 Alan: Well, get out twenty-four ones.
- 9.2.41 Erik: I think we need twenty-four ones.
- 9.2.42 Alan: Mmm hmm
- 9.2.43 Erik: One, two three four five six seven, I'll just take out as many as possible
- 9.2.44 T/R 1: [To Erik and Alan] I have a question for both of you. I've watched you do this in the tapes at breakfast this morning, so I feel very close to your solution, Erik, and Alan, but I, I have another question. While you're building this, I'd like you to build the other model you also made.
- 9.2.45 Erik: That was
- 9.2.46 Alan: Oh, yeah, the two browns, remember?
- 9.2.47 Erik: Yeah
- 9.2.48 Alan: One brown, two, yeah it was the two
- 9.2.49 Erik: One of those
- 9.2.50 Alan: Yeah, one
- 9.2.51 Erik: Something like that.
- 9.2.52 T/R 1: Ok, I'd like you to build the other model, and then I want to ask you a question about your two models. Try to remember what
- 9.2.53 Alan: Yeah it was the two browns I think.
- 9.2.54 T/R 1: Why do you think it was the two browns?
- 9.2.55 Alan: Because two browns, you would be able to third it and fourth it. So, let's see. One, two
- 9.2.56 Erik: Don't take any whites, though. Because I need all the whites possible.
- 9.2.57 Alan: I know.
- 9.2.58 T/R 1: We can get some more.
- 9.2.59 Erik: Plus there are probably no whites left in there.
- 9.2.60 Alan: Let's see,
- 9.2.61 Erik: There are two whites, don't take any of them. I need twenty-four of em. Now we know that there's twenty four...
- 9.2.62 T/R 1: Ok, build the other model and then when you're done, call me back.
- 9.2.63 Erik: Twenty-eight whites and one fifth.
- 9.2.64 Alan: I need the um
- 9.2.65 Erik: Yeah, no
- 9.2.66 Alan: Give me two dark greens, no, three, make it three, um, blacks that might do it. Yeah, three blacks thirded this.
- 9.2.67 Erik: No, no, cuz blacks are bigger than dark greens.
- 9.2.68 Alan: Oh yeah, dark greens, get me three dark greens

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- 9.2.69 Erik: No, dark greens don't work.
- 9.2.70 Alan: Those are two browns? Oh yeah.
- 9.2.71 Erik: Maybe.
- 9.2.72 Alan: Oh I know. Oh, now I remember, it was a train of two browns and a red.
- 9.2.73 Erik: Yeah, that's what I remember - don't take a red, no, not from there! [Erik has built a model of an orange and red train, three purple rods, four light green rods, six red rods, and twelve white rods]
- 9.2.74 Alan: Greg, can you spare some of the red? Oh never mind. I'll just take it. We don't ask. [laughs]
- 9.2.75 Erik: Ok. Here, so brown, two browns, a red, and yellows were the thirds, I think.
- 9.2.76 Alan: No, fourths.
- 9.2.77 Erik: No.
- 9.2.78 Alan: Purples were, no, dark greens thirded it.
- 9.2.79 Erik: Maybe, uh yea I guess. Could you spare us three, uh, three dark greens, Greg? We need-
- 9.2.80 Alan: I can't get any rods these days. We're low on 'em. We're low. We low on supplies. Oh. Oh great.
- 9.2.81 Erik: There's nothing left in the boxes, there's like absolutely nothing in the boxes!
- 9.2.82 Alan: There are none up there.
- 9.2.83 Erik: Oh, here's another dark green!
- 9.2.84 Alan: Oh, good good good
- 9.2.85 Erik: We need two.
- 9.2.86 Alan: Uh, I think that might do.
- 9.2.87 Erik: I don't know. Where's the half?
- 9.2.88 Alan: [mimicking] I don't know, know.
- 9.2.89 T/R 1: Alen There may be some more boxes in the back.
- 9.2.90 Erik: More boxes in the back? Aren't there also some bags?
- 9.2.91 Alan: Bags of Cuisenaire rods?
- 9.2.92 Erik: We need
- 9.2.93 17:18 Alan: Sheesh, we're wasting trees, three pieces of paper? Wow.
- 9.2.94 Erik: David, can you spare us three dark greens? Or two, one rather. Got 'em.
- 9.2.95 Alan: Got 'em. Oh good, we got three. Let's see if that thirds it. Hey, come on no peeking, no peeking, you have eyeballitis.
- 9.2.96 Erik: Yah.
- 9.2.97 Alan: Ok, it works.
- 9.2.98 Erik: Ok, let's see, fourths should be,

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9.2.99 Alan: Fourth would be the purples.

9.2.100 Erik: Yeah, that's what I was thinking. Two, three

9.2.101 Alan: [makes noise]

9.2.102 Erik: No, ok.

9.2.103 T/R 1: If you don't have enough of the little rods, you can imagine them, or what you could do, besides imagining them you could take some of them off, once you put twenty-four we believe you, right? Here are some more of them.

9.2.104 Alan: Now let's see. What fourths this?

9.2.105 Erik: We're trying to figure out. It wasn't the purple but

9.2.106 Alan: It can't be. Oh, now I remember the combo.

9.2.107 Erik: What was it? No way, no way, no!

9.2.108 Alan: It has to be. The yellows did have some part in this.

9.2.109 T/R 1: Can I make a suggestion, gentlemen?

9.2.110 Erik: Uh huh. I think it was one brown plus a red.

9.2.111 19:17, Fig 1 T/R 1: My suggestion is, you have the answer to your question if you carefully study what you built here. If you carefully study this, and study what you did here, you may have the answer to it. If you think about how you built your one here, that should help you, just think about it. [turns attention to another student] Yes, sir.

9.2.112 Alan: Hold it

9.2.113 Erik: [makes noise]

9.2.114 Alan: There. Subtract two from each of those things. What would you get? Two from the purple would be a red, two from an orange would be a blue, two from a brown, would be a

9.2.115 Erik: A brown.

9.2.116 Alan: Yeah, Right! So two browns and a red must be the answer, right?

9.2.117 Erik: No.

9.2.118 Alan: Oh.

9.2.119 20:12 Erik: Just try one brown

9.2.120 Alan: One brown.

9.2.121 Erik: Let's see what does it, sorry.

9.2.122 Alan: Oh, wait, wait, wait, wait!

9.2.123 Erik: Light greens would take a part in it. No, it's one brown and a red. The purples wouldn't take a part. Wait...

9.2.124 Alan: Fourths, maybe we could try a red? Yeah, exactly!

9.2.125 Erik: Four Blacks. One, two, three... Let's see, we don't need halves, we need, wait, maybe it was two browns and a red.

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- Two browns and a red, then two from a brown would be a black, wouldn't it? No
- 9.2.126 21:20 Alan: No, dark green, d.g.
- 9.2.127 Erik: Wait, yeah, wait
- 9.2.128 Alan: Yeah, dark green, get me three dark greens. Alright
- 9.2.129 Erik: We did this already now what's the fourths? Ok, fourths there are dark greens, two from the dark greens would be a, a
- 9.2.130 Alan: A light, purple. Purple would fourth this. You see? One, two, three, four.
- 9.2.131 Erik: And it's the same, and it's gotta be a - the light green's smaller,
- 9.2.132 Alan: Hmm... Hold it, look at this. Two browns, which would equal up to ten, wouldn't it?
- 9.2.133 Erik: No.
- 9.2.134 Alan: Yes, two down from uh, the uh brown. So this is ten, twelve. Half of twelve would be six. We need something that, these are four each.
- 9.2.135 Erik: Those are six.
- 9.2.136 Alan: Right, now all we need to do is divide twelve.
- 9.2.137 Erik: It's not twelve, it's not twelve, that is a, that's a, two down from ten would be eight. Eight, twelve,
- 9.2.138 Alan: Twenty-two. That's twenty-two
- 9.2.139 Erik: It can't be twenty-two.
- 9.2.140 Alan: Twenty-two divided into four parts
- 9.2.141 Erik: No wait, no wait. Eight sixteen eighteen, it would be eighteen, because eight sixteen, seventeen, eighteen. Eighteen divided by six
- 9.2.142 Alan: Would equal
- 9.2.143 Erik: Wait
- 9.2.144 Alan: Eighteen divided by six would equal two.
- 9.2.145 Erik: No, no, no, no, no
- 9.2.146 Alan: No, twelve divided by six would equal two.
- 9.2.147 23:41 Erik: But,
- 9.2.148 Alan: Oh,
- 9.2.149 Erik: That's impossible.
- 9.2.150 Alan: Impossible? But totally unexpected. B-L-A-C-K-S. Get me blacks.
- 9.2.151 Erik: Oh, I have three, or four. [hands blacks to Alan]
- 9.2.152 24:34, Fig 2 Alan: There [Alan has built a model of two browns and a yellow and three black rods]
- 9.2.153 Erik: What are you doing? That's not what we...

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- 9.2.154 Alan: Sure
- 9.2.155 Erik: No it was, No, it was two yellows and a red! Remember? It was two yellows and a red?
- 9.2.156 Alan: Oh, yeah... No! It was an orange.
- 9.2.157 Erik: No it wasn't
- 9.2.158 Alan: Look: two yellows and a red would equal an orange and a red.
- 9.2.159 Erik: No it wouldn't
- 9.2.160 Alan: Yeah it would
- 9.2.161 Erik: No it was like that and then the light greens
- 9.2.162 Alan: Were the fourths
- 9.2.163 25:02, Fig 3 & 4 Erik: Told ya!
- 9.2.164 Alan: Hold it, let me see. Look, there's a way you can eliminate these two yellows. There we go! That was an adventure.
- 9.2.165 Erik: Just put these along with this. [Erik moves this new model of an orange and red train, four light green rods, and three purple rods, next to his other model]
- 9.2.166 Alan: We have this model. You busted it!
- 9.2.167 Erik: No I didn't, I can make it again.
- 9.2.168 Alan: Well, you'll back the other model, because we might have, we do have enough. Good. Erik, come on, Dr. Maher is here. We done. We done.
- 9.2.169 26:20 T/R 1: Gentlemen, gentlemen.
- 9.2.170 Alan: Ok, that's the second one.
- 9.2.171 T/R 1: Oh, what do we have here? Tell me what we have here.
- 9.2.172 Both: An orange and a red
- 9.2.173 Alan: And purples for thirds
- 9.2.174 Erik: And three purples
- 9.2.175 Alan: And light green for fourths.
- 9.2.176 T/R 1: Ok, right.
- 9.2.177 Alan: And, um, here how I used to figure it out.
- 9.2.178 Erik: Twelfths! Oh no, those are singles
- 9.2.179 T/R 1: Honestly, Erik, I could imagine if you explained to me what I'm supposed to imagine.
- 9.2.180 Alan: Ok.
- 9.2.181 T/R 1: Ok? I'll try real hard, but I'll try to imagine
- 9.2.182 Alan: Suppose there are twelfths under that.
- 9.2.183 T/R 1: I can imagine that.
- 9.2.184 Alan: And you took out two of those purples and three light greens
- 9.2.185 T/R 1: I could imagine



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- 9.2.186 Alan: It would take one of those twelfths to fill in the gap between the, between the um um
- 9.2.187 Erik: See?
- 9.2.188 Alan: Two thirds and three fourths
- 9.2.189 T/R 1: I see that.
- 9.2.190 Erik: And we came to up here
- 9.2.191 Alan: So Three fourths is bigger than two thirds by one twelfth
- 9.2.192 Fig 5 Erik: And what we came to up here, two thirds and three fourths, it would be bigger by one twelfth or-
- 9.2.193 Both: Two twenty-fourths.
- 9.2.194 Erik: Because two of 'em equal up to a red like the orange and the
- 9.2.195 T/R 1: Why is it a red here and why is it a white here?
- 9.2.196 Alan: Well
- 9.2.197 Erik: Well, because, see each model is different
- 9.2.198 T/R 1: In what way?
- 9.2.199 Erik: Because this model is bigger than this model
- 9.2.200 Alan: Erik! You could put the reds on that model and make it sixths!
- 9.2.201 Erik: But then it would be- so why would we need sixths on that model?
- 9.2.202 Alan: Oh yeah, you're right. So either it's one twelfth or one twenty-fourths
- 9.2.203 Erik: Two twenty-fourths
- 9.2.204 Alan: Two twenty-fourths on this one. This is probably the only model that can get the twenty-fourths cuz you can't, you'd have to halve each white to get twenty-fourths there.
- 9.2.205 28:07 Erik: But what if you get three three, um uh, three oranges together
- 9.2.206 Alan: We tried that already
- 9.2.207 Erik: No we didn't we could get like fiftieths.
- 9.2.208 T/R 1: You think it would be fiftieths if there would be three oranges?
- 9.2.209 Erik: Well, I don't know exactly but it would be a lot.
- 9.2.210 T/R 1: Do you still expect that you would get the same answer?
- 9.2.211 Erik: Well, we can divide it.
- 9.2.212 Alan: Looking at this it would not be fiftieths.
- 9.2.213 T/R 1: Why not?
- 9.2.214 Alan: I'm imagining a this (takes another orange) instead of the purple there.
- 9.2.215 T/R 1: Instead of the purple?
- 9.2.216 Alan: It would take another six of those so it would only be thirtieths

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9.2.217 T/R 1: I'd like you to try that other model.

9.2.218 Alan: Three oranges?

9.2.219 28:42 T/R 1: Well whatever you think it is, um, I'd like you find a third model and I think Dr. Martino said to think big. I'd like you to find a third model thinking big.

9.2.220 Alan: Ok

9.2.221 Erik: We could think real big.

9.2.222 T/R 1: And see what you come up if you work on that.

9.2.223 Erik: Dr. Martino said the key is think big, so

9.2.224 T/R 1: Well, maybe, we'll see if it works.

9.2.225 Erik: So now were gonna think real big!

9.2.226 Alan: Yeah, four of 'em

9.2.227 Erik: Three, give me three of these. Let me just put these back...

9.2.228 Alan: Four of 'em that would be right!

9.2.229 29:07 Erik: Fiftieths, I told ya.

9.2.230 Alan: Four of 'em, make four, then it would be two yellows

9.2.231 Erik: Friar tuck, may I have them? I think Friar Tuck's going to have to go around

9.2.232 Alan: Two four six eight, there would be eighths

9.2.233 Erik: Alan, Friar Tuck's have to go around, ok?

9.2.234 Alan: Uh, what do you need?

9.2.235 Erik: I'm probably going to need whites.

9.2.236 Alan: How many?

9.2.237 Erik: Well, it's going to be fiftieths, and we only have twenty-eight.

9.2.238 Alan: Ok.

9.2.239 Erik: So we're going to need about fifty thousand. We're going for three.

9.2.240 Alan: I think Erik you better go.

9.2.241 Erik: No

9.2.242 Voice: You don't need fifty singles. We trust you on that.

9.2.243 Alan: Ok.

9.2.244 Voice: Because otherwise no one's going to have any.

9.2.245 Alan: Right.

9.2.246 Erik: I know what the thirds are.

9.2.247 Alan: What?

9.2.248 Erik: Oranges

9.2.249 Alan: Oranges?

9.2.250 Jessica: Are you figuring out the big one again?

9.2.251 Erik: No

9.2.252 Alan: No, we're trying to...

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9.2.253 Erik: Three oranges.

9.2.254 Alan Erik, use the yellows. Think big.

9.2.255 T/R 1: A suggestion I have, Alan and Erik, if you can find another table who's solving the same problem then maybe you can combine

9.2.256 30:12 Erik: Well, we need a lot more Cuisenaire Rods. Well, let's work with three and then we'll do four.

9.2.257 Alan: Right.

9.2.258 Erik: Ok, what would be the thirds. Thirds would easily be the oranges. One two three.

9.2.259 T/R 1: Well, just build your big model and we could use Meredith and David's smaller model. And then you could come together to put all your models together.

9.2.260 Alan: And then show them on the overhead?

9.2.261 T/R 1: Yes.

9.2.262 Alan: Ok.

9.2.263 T/R 1: So work on the big model. See what you can do.

9.2.264 Alan: Erik,

9.2.265 Erik: we need oranges. [to next group] Do you have three oranges we can borrow?

9.2.266 T/R 1: Here

9.2.267 Erik: Oh, good. I'll just pour them into the little - Ah!

9.2.268 Alan: Ok,

9.2.269 Erik: Now we need,

9.2.270 Alan: Ok, perfect! There are thirds

9.2.271 Erik: Right, now fourths, would be two smaller than an orange, a brown, no, yeah! Three, no that's too big. Two smaller, what's two smaller than a brown. Not a black, but a yellow, no, not a yellow

9.2.272 Alan: Yes,

9.2.273 Erik: No

9.2.274 Alan: A dark green - look it look it for your answer.

9.2.275 Erik: The dark green would be the fourths?

9.2.276 Alan: Mmm hmmm. Believe it or not, they are. They might be the fifths.

9.2.277 Erik: They're the fifths. Then what would be the-

9.2.278 Alan: Blues would be the

9.2.279 Erik: This would only be thirty. This would only be thirty because ten twenty thirty.

9.2.280 Alan: Thirty plus twelve. Forty-two

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- 9.2.281 Erik: Wait a minute. Since we got these two packs, couldn't we have, Alan, couldn't we have like, um, Alan, couldn't we have, ten twenty thirty forty fifty sixty, wait, ten twenty thirty forty fifty sixty seventy if we all put them
- 9.2.282 Alan: Erik, those aren't tens, those are twelves
- 9.2.283 Erik: Yeah those are tens.
- 9.2.284 Alan: You know what tens are? The browns.
- 9.2.285 Erik: Look at this.
- 9.2.286 Alan: Prove it.
- 9.2.287 Erik: Look at this
- 9.2.288 Alan: Put ten up to that.
- 9.2.289 Erik: Ok.
- 9.2.290 33:03 Alan: Ten. Put ten. Put ten up to that. [Erik does so] Maybe it is ten. Ok, ten twenty thirty forty fifty, it would have to be ten,
- 9.2.291 Erik: Ten twenty thirty forty fifty sixty seventy
- 9.2.292 Alan: Here we go again.
- 9.2.293 Erik: Let's just start with thirty.
- 9.2.294 Alan: Yeah, let's eliminate two of the tens.
- 9.2.295 Erik: Ok, what would be the fourths?
- 9.2.296 Alan: Fourths of that
- 9.2.297 Erik: Brown could be in here somewhere
- 9.2.298 Alan: Nope, nnnnope
- 9.2.299 Erik: Blues
- 9.2.300 Alan: Nope. Too big. Eeew! Erik, wipe those rods off immediately. Erik, you're thinking. Hold it...
- 9.2.301 34:21 Erik Blacks
- 9.2.302 Alan Blacks blacks blacks blacks, right right right, go go go go go. Yup, told you. They're one short. Oh
- 9.2.303 Erik: Four long? No. Hah. Alan. Whoops, never mind, that's a five. We didn't forget how to make a big one. We're just experimenting. Perfect! Now just do that, one two three, [noise] No, one larger than this would be the [noise. Erik has built a model of three oranges and a dark green] I got the fourths.
- 9.2.304 35:47, Fig 6 Alan: Now make the thirds.
- 9.2.305 Erik: Ok, what if we did this? I bet I could make the thirds
- 9.2.306 Alan: I think uh, yo, Erik, I think we were just tipped. Erik, come here, go go go. Go go. Alright.
- 9.2.307 Erik: Bigger than a dark green, well, how much bigger do I need it then, how much bigger can it get?
- 9.2.308 Alan: Erik, hold it, the thirds.

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9.2.309 Erik: I am trying to do something.

9.2.310 Alan: Thirds thirds thirds. Wait a second, three oranges would have to be the thirds.

9.2.311 37:00 Erik: What? What?

9.2.312 Alan: [looking at model that Jessica and Andrew built] That would be two oranges and a yellow. Two oranges and a purple

9.2.313 Erik: We already did that.

9.2.314 T/R 1: How are you gentlemen doing, did you get another new model?

9.2.315 Alan: Yeah

9.2.316 Erik: Not exactly, actually. You see

9.2.317 T/R 1: You might want to study, you might want to study Andrew's model to see what you have to do to make it bigger.

9.2.318 Erik: Well, that's the exact same thing we did. We did two oranges and a purple.

9.2.319 T/R 1: Yeah, but I want you to make one bigger than his.

9.2.320 Erik: We're trying, but we can only divide it into one two three four fi- fifths. I can divide it into thirds, but I can't divide it into fourths.

9.2.321 T/R 1: Well, maybe you gotta make it bigger. See my problem? This is a good challenge for you two. Study that, yeah.

9.2.322 Erik: Those are twelfths.

9.2.323 Alan: Make six of those and it would be ten greens.

9.2.324 Erik: We want thirds and fourths, not tens.

9.2.325 T/R 1: I wonder if Meredith and David made any progress. Meredith and David [walks away]

9.2.326 38:33 Alan: Thirds. Erik, there's one prob. Using oranges, you can't third. You can't third, look, even if you subtracted two you couldn't third that. Because orange is twelve, there's five.

9.2.327 Erik: Oranges are tens!

9.2.328 Alan: I know, tens, you can make it into fourths but you couldn't third it.

9.2.329 Erik: Wait you gave me, oh no.

9.2.330 39:12 Alan: You just gave up

9.2.331 Erik: Yup.

9.2.332 Alan: Hold on a sec, look, look, you take that off, you could use that

9.2.333 Erik: That's way too big, Andrew, I don't think you can divide it into anything

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- 9.2.334 Andrew: Yeah, if you make two browns, two blues are thirds. If you can make a train for a whole you can make a train for a third and a fourth.
- 9.2.335 Erik: Ohhh!
- 9.2.336 [taken from other view, but can be heard partially here]  
That's very interesting. That's an interesting theory. Why don't you test the theory with Michael and Alan, I think they would like to hear this theory. Would you like to hear - I think David has a theory - why don't you come over here. They have an interesting -
- 9.2.337 Erik: So do they have a theory.
- 9.2.338 T/R 1: David has an interesting theory, I don't know if Meredith heard it, tell them his theory, now listen carefully, Jackie, you want to hear this theory? [Andrew has built a model of four oranges and two purples, and six browns.]
- 9.2.339 Andrew: [to Jessica] See? Two of these are thirds, and that's a one third, third, third. [Andrew has originally made his train of "one" as two oranges followed by a red and then that pattern repeated. He now moves the reds to the end. He then takes eight green rods and puts them down] Erik, I figured out the thirds, I just need the fourths.
- 9.2.340 41:21 Erik: You did? How did you figure out the thirds?
- 9.2.341 Alan: Ok, Erik. Get ready for big city play dude, big time.
- 9.2.342 41:51, Fig 7 Andrew: Erik, I made it!
- 9.2.343 Erik: Wow, now divide it into twelfths and see what you can divide by - [Erik joins Andrew. Camera focuses on David, Meredith, Erik and Alan on the floor.]
- 9.2.344 Alan: OK, Here are the rods
- 9.2.345 Erik: I'm working here. You could do it! You could do it! Andrew did the same, Andrew did the same model. They did the same model. Ok, this is what you do. You do three oranges, you do actually you do three oranges and two purples. Three oranges
- 9.2.346 Alan: Four oranges
- 9.2.347 Erik: Three oranges!
- 9.2.348 Alan: Ok
- 9.2.349 Erik: Three oranges and two purples.
- 9.2.350 Alan: Two purples would just be a brown.
- 9.2.351 Erik: An then... a brown? No it wouldn't, yeah it would, and then you could make a train for the thirds. [talk about whose mat

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is who's] Ok, and then the browns, two browns would make a train for one third

9.2.352 Alan: Right,

9.2.353 Erik: And then,

9.2.354 Alan: Woo, woo, woo, woo

9.2.355 43:40 Erik: And then two more browns would make another train for thirds. One, two, I know. No, wait, no, it wouldn't be browns, it would be blacks.

9.2.356 David: Could I just do what I was thinking of? Could I just

9.2.357 Erik: No they're not, look, it'd be blue and a purple or a blue and a

9.2.358 David: Could I just make something?

9.2.359 Alan: Hey you're robbing me.

9.2.360 Erik: Everyone's robbing you, remember?

9.2.361 David: Could I have some

9.2.362 Erik: Me and David will work together.

9.2.363 David: Could I have some?

9.2.364 Meredith: I'm working with Erik.

9.2.365 David: Can't I just use some of the blocks over there? I brought it over Meredith.

9.2.366 David: Can I have some?

9.2.367 Alan: Check it out

9.2.368 Erik: No, I'm just kidding

9.2.369 Alan: Check it out.

9.2.370 Erik: Now divide it into thirds

9.2.371 Alan: Hmmm

9.2.372 Erik: You can't

9.2.373 Meredith: I have and idea.

9.2.374 Alan: Wow, something just popped into my head

9.2.375 Erik: Me too

9.2.376 David: Something just popped into my head.

9.2.377 44:56 Alan: The bigger you make the model, you can't third it.

9.2.378 Erik: No no no no no, can I have these?

9.2.379 Alan: [continuing] You can't third something like this. You'd need colossal rods.

9.2.380 Erik: Like the ones over there?

9.2.381 David: I know something, alright?

9.2.382 Alan Impossible. That'd just like one dark green.

9.2.383 David Can I um do something?

9.2.384 Erik: Hold on, let me do something [start fighting over rods] Could I have the blue

9.2.385 Alan: Erik! You can't third that big orange model.

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9.2.386 Erik: You want to make a bet? I bet I can.

9.2.387 Alan: You can't

9.2.388 Erik: I bet I can. Oranges

9.2.389 Alan: Because if you use more. Using oranges, if you use three oranges, you won't be able to third it. You won't be able to third it!

9.2.390 Erik: This is what I was thinking. One, two three. Oh contraire... It needs to be, let's see, how much smaller?

9.2.391 46:05 Alan: Look you can't third it, you fourthed it but you can't third it.

9.2.392 Erik: Ok, let's see, four one two, easily how you can do it.

9.2.393 Alan: Third it then.

9.2.394 Erik: What?

9.2.395 Alan: Third it then.

9.2.396 Erik: What do you mean?

9.2.397 David: Who took my thirds? I was using them.

9.2.398 Erik: Me! I think, no it wasn't me. It was Alan.

9.2.399 Alan: Make three blues and train it. Then you could use those

9.2.400 Erik: What do you think I was thinking of? Give me my rods back. Stop!

9.2.401 David: Meredith, can I have my rods? I brought them over.

9.2.402 Erik: Alan, you're stealing from, no no no, Alan you're stealing from us! No.

9.2.403 Meredith: Oh, oh! Did you just take one of my blues

9.2.404 Alan: No

9.2.405 Erik: Yeah. And for the thirds the thirds can easily be done by the blues

9.2.406 David: I have an idea.

9.2.407 Erik: I've got a good idea.

9.2.408 David: I've got a better idea.

9.2.409 Erik: The thirds, and then how much room do we have left? We have one blue left which is nine. One two three four five six seven eight nine.

9.2.410 David: Just listen out.

9.2.411 Meredith: Me need a brown rod

9.2.412 Erik: It all works out.

9.2.413 Alan: You know what you could try? Use three blues and the light green then use the oranges to third it then you could fourth it easily

9.2.414 Erik: Now.

9.2.415 David: I already have a third. See just put down the purple and I took off the green. Here's what I made.



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- 9.2.416 Alan: Look it. [to Meredith] You have any blues?
- 9.2.417 Erik: Yeah but she's not going to give them to you.
- 9.2.418 Alan: And the light green. Easily your thirds can be used.
- 9.2.419 Erik: Perfect, I did it! Hello Alan, I did it!
- 9.2.420 Alan: You fourthed it too?
- 9.2.421 Erik: Yup! One two three four
- 9.2.422 Voice: Can you third that?
- 9.2.423 Erik: I thirded it. One two three and then plus nine other of those, which would be one two three four five six seven eight nine. So it's just like making a new rod.
- 9.2.424 Alan: Fourthing it might be.
- 9.2.425 Voice: Can you run it by me again? I'm not quite following that.
- 9.2.426 48:37 Erik: Ok. I have the three of 'em, and then I put nine other ones which would equal another blue, so if I thirded it, I would add one to there, one to there, and one to there, which would be three. And then four five six seven eight nine. So it's like adding another blue, but I'm making a new rod. [Erik's model is -Three orange rods and a dark green rod, a train of four blue rods, and a train of three blue rods and nine white rods]
- 9.2.427 Voice: Ok, can you set that up in a different way?
- 9.2.428 Erik: Well, in thirds
- 9.2.429 Voice: Use the same pieces, but can you set it up a little differently?
- 9.2.430 Meredith: Oh, I have an idea, put the three next to that, and then the three next to that and the three next to that.
- 9.2.431 Erik: Huh?
- 9.2.432 Meredith: I'll show you what I mean. [Meredith places three white rods after each blue rod.
- 9.2.433 Erik: How can we make it bigger than him? He did the exact same thing.
- 9.2.434 Meredith: There!
- 9.2.435 Erik: Ohhhh!
- 9.2.436 Meredith: There! Get it?
- 9.2.437 49:54 Erik: Ohhh! see, there are there to that, three to that, and three to that, so it's like, it's a blue plus one would be an orange, plus another would be a new rod, plus another would be a new rod, and if you have another one, it'd, you'd, you're just making new rods. Because if you add one of those to that, it'd be an orange, but then you add another two it'd be bigger than an orange.
- 9.2.438 Voice: I got you.
- 9.2.439 50:25, Fig 8 David: Told you I got it.

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- 9.2.440 Meredith: Or you could just take the oranges and do that.
- 9.2.441 Erik: No, those were uh
- 9.2.442 David You could take out the three six nine
- 9.2.443 Meredith: You could take out the orange and use two ones.
- 9.2.444 Erik: I think the greens would be sixteenths, not
- 9.2.445 David You could take out the three six nine and put a blue in there
- 9.2.446 Meredith: Orange and six ones. Oh, wait a second! Aren't these nines? Aren't these nines, right?
- 9.2.447 Erik: Yeah the blues are nines.
- 9.2.448 Meredith: And these are tens, right?
- 9.2.449 Erik: Yes, those are tens.
- 9.2.450 Meredith: But, if they're tens, why are they bigger than these?
- 9.2.451 Erik: Huh?
- 9.2.452 Meredith: See what I mean? You put the, put the four orange
- 9.2.453 Erik: You know why the blues bigger than 'em? Because they have the three whites added
- 9.2.454 Meredith: But the orange is bigger!
- 9.2.455 Erik: Of course, the orange are ten, those are nine.
- 9.2.456 51:26 CT: I don't want to break your train of thought, but what's happening here?
- 9.2.457 Erik: Well, see, we took the three oranges and the dark green to be one, and then the four blues to be um the fourths, and down here we took three blues and then uh nine whites and we took three whites which would go to that one, so we're making a new rod, because if you add one it would be an orange, but if you add to other ones, it would be bigger than an orange, so we're making a new rod there and we do the same here and the same here, so we're making new rods for thirds.
- 9.2.458 CT: Ok.
- 9.2.459 Erik: That's basically what we're doing.
- 9.2.460 CT: You have to.
- 9.2.461 Erik: I don't, I don't really understand what Dave's doing. That's the only problem. Actually, no, I do. He's calling two browns, two blacks, and two blues a one.
- 9.2.462 Meredith: Yeah, cuz that was twice the other
- 9.2.463 Erik: Yeah, and then the light greens are the twelfths and those
- 9.2.464 David: I think that'd be sixteenths though
- 9.2.465 Erik: Yeah, and the reds would be the twenty-four- the twenty-fourths. The reds would be the twenty-fourths and the whites would be the forty-eighths. Because he doubled everything.
- 9.2.466 Meredith: Where are the thirds? Where are the fourths?

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9.2.467 Erik: Exactly.

9.2.468 David: I'm just working on this.

9.2.469 Erik: He's working on that. Ok!

9.2.470 Meredith: He's just working on the model

9.2.471 52:47 Erik: Dave, isn't this basically what we came here for?

9.2.472 CT: [talks to other students]

9.2.473 Erik: Dave, isn't this basically what we came here for?

9.2.474 David: Why did you do that, Alan?

9.2.475 Alan: I'm getting it lined up. Trying to get it lined up.

9.2.476 Erik: So we don't need this, basically we don't need all this. We can just push that aside and work with Dave's. Isn't this basically what we came here for, David?

9.2.477 David: Yeah, I know, that's why

9.2.478 Erik: Everyone's just trying to make another model.

9.2.479 CT: Basically you came here for what?

9.2.480 Erik: Basically we came here to discuss David's original model.

9.2.481 CT: And then you built something else.

9.2.482 Erik: Yeah.

9.2.483 David: Yeah, cuz I told everybody and then she said to go over there and build Dave's model, and then

9.2.484 Erik: We lost the point for some reason.

9.2.485 CT: Ok, but I don't think David did. Did you?

9.2.486 Erik: No, David's did, but David's like, here let me do this.

9.2.487 CT: David, how about you explain to me what you're doing so I can understand your thinking.

9.2.488 53:40 David: Well, before Meredith built this other thing and then she had the reds were one twelfth and then the whites were one twenty-fourth, but then.

9.2.489 Erik: We built that, me and Alan built that originally.

9.2.490 David: Yeah, and Meredith, Meredith did too, and then um, uh, so then she, she thought to think of a bigger model, then I thought that then maybe the greens would be something like one twelfth but I figured out that would be sixteen when I put them up there, and

9.2.491 CT: Right.

9.2.492 Erik: No it wouldn't because you still have some room.

9.2.493 David: No,

9.2.494 54:20 Erik: I think

9.2.495 David: No it's just that that piece is hanging out, um, then I thought the reds would be one twenty-fourth and the whites might would one forty-eighth because I just doubled it.

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9.2.496 CT: Did it work out?

9.2.497 David: What?

9.2.498 CT: Did it work out? Did you find what you thought you would find?

9.2.499 David: Um, well, not with the greens, that turned out to be one sixteenth

9.2.500 CT: The greens turned out to be what, sweetheart?

9.2.501 David: One sixteenth.

9.2.502 CT: And the reds came out to?

9.2.503 David: I'm working on that right now.

9.2.504 CT: Oh, ok. I'm sorry.

9.2.505 Erik: What about the purples? The purples, the purples might come out to be

9.2.506 David: Yeah they might be one-

9.2.507 Erik: I think the purples would do that.

9.2.508 David: Maybe it would be something else.

9.2.509 55:03 Erik: The purples would be one twelfth.

9.2.510 David: Alright, so now

9.2.511 CT: This is so interesting, where are you going with this, then?

9.2.512 David: What?

9.2.513 CT: Where are you going with it? I mean, this is very interesting, I'm enjoying it very much, you put a lot of work into it.

9.2.514 Alan: This isn't going to be able to fit on notebook paper.

9.2.515 CT: We can take, listen, we can take this and paste it together and put your work on it.

9.2.516 Erik: Well, it barely even fits on this!

9.2.517 CT: Well, you have more than one piece there, so there's no problem there, don't worry about that.

9.2.518 Erik: I mean, if it doesn't fit on this, of course it can't fit on a single piece of notebook paper, but if we put a couple of pieces together it'd fit.

9.2.519 CT: It's ok, we can set up a model. What should we?

9.2.520 David: I think, maybe I counted wrong but that, but I counted it to be one twenty-third. Maybe I'll count again.

9.2.521 CT: Ok, let's see. See if you have it even.

9.2.522 Erik: One two three, four, one two three

9.2.523 55:59 T/R 1: They don't look lined up to me, David. David, I'm not convinced they're lined up.

9.2.524 Erik: Eleven twelve thirteen fourteen fifteen sixteen

9.2.525 Alan: Dave, you have something wrong, you need another

9.2.526 Erik: Twenty-three. You need to line them up.

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9.2.527 Alan: Here, you've got, yeah, you need another one of that.

9.2.528 T/R 1: How about a ruler, would that help? A yardstick, behind the board there? A yardstick might help.

9.2.529 Erik: Yeah [gets up].

9.2.530 T/R 1: See it over there?

9.2.531 Alan: Now, push, push, the reds down.

9.2.532 Erik: Just push em in, and then you can get one more.

9.2.533 Alan: There.

9.2.534 Erik: Now put one more on, just put one more on.

9.2.535 56:36, Fig 9 Alan: Take a yardstick and flatten the whole thing out.

9.2.536 Erik: What do you mean, flatten it out?

9.2.537 Alan: It's all wavy.

9.2.538 Meredith: Yo!!! I just worked [inaudible]

9.2.539 Erik: No, I mean, it's not ok, cuz, no offense Meredith, but isn't this called the major model we were supposed to be working on?

9.2.540 David: That's what we're doing. That's why we came over here.

9.2.541 Alan: Ok. Pointless. Use the purple!

9.2.542 Erik: One two three four five six seven eight nine, ten, eleven, twelve, thirteen, fourteen fifteen, oops, sorry. I just think that the purples

9.2.543 David: We need the purples

9.2.544 Alan: I know, I'm giving them to you. Is that enough?

9.2.545 Erik: One two three four five six seven eight nine ten

9.2.546 David: This is going to be twelve. I know it.

9.2.547 Erik: Eleven Twelve

9.2.548 David: I know it. The purples

9.2.549 Erik: Two three four

9.2.550 David: Ok, let me do it.

9.2.551 Erik: five six seven eight nine ten eleven twelve. There we go. Now we can just knock all those.

9.2.552 57:52 Meredith: [Alan begins to straighten the model with the yardstick] No, that side's

9.2.553 Erik: You don't really need- Wait a minute, now I just gotta do the thirds and the fourths.

9.2.554 David: Don't touch anything now.

9.2.555 Erik: One two three four five six

9.2.556 Fig 10 David: Don't touch anything. You can just count. [David gets up and leaves view of camera for a minute and returns] alright, let's see I think the ones would be one forty-eighth

9.2.557 58:44 Erik: Wait, four, eight twelve, just count by fours, cuz.

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- 9.2.558 David and Erik: Two four six eight ten twelve fourteen sixteen eighteen twenty twenty-two twenty-four twenty-six twenty-eight.
- 9.2.559 David: Thirty.
- 9.2.560 Erik: Two four six eight ten twelve fourteen sixteen eighteen twenty twenty-two twenty-four twenty-six twenty-eight thirty, thirty-two, thirty-four, thirty-six, thirty-eight, forty, forty-two, forty-four, forty-six, forty-eight. Yep, forty-eight.
- 9.2.561 59:23 T/R 1: Are you surprised that it's forty-eight?
- 9.2.562 Erik: No, not really
- 9.2.563 David: No, that's what I thought it would be.
- 9.2.564 T/R 1: That's what you guessed? So in other words, you were able to build what you thought, what you predicted. Are you going to be able to write this up?
- 9.2.565 David: Um, well, not draw it, maybe not
- 9.2.566 T/R 1: Maybe sketch it, maybe you want to take some notes on your diagram before it ends. What do you think, Meredith? You think you made another, you made a different model. Ok, you might want to take some notes to sketch it to you remember what you did. So you can start
- 9.2.567 Erik: But how would we sketch it?
- 9.2.568 David: Well I was surprised because I thought the greens were the purples one twelfth.
- 9.2.569 Erik: So I think what I'm gonna do
- 9.2.570 T/R 1: So you think the purple's one twelfth - is there another name for that purple?
- 9.2.571 Erik: Um, one, one
- 9.2.572 T/R 1: Meredith always like to have other names for these
- 9.2.573 Erik: One twelfth
- 9.2.574 T/R 1: I know, that's one name, one twelfth. Is there another number name for the purple?
- 9.2.575 Erik: One fourth, no. I mean, uh, what's it called. Wait,
- 9.2.576 T/R 1: If you were using-
- 9.2.577 Erik: One whole!
- 9.2.578 T/R 1: If, let me ask you this
- 9.2.579 Erik: One whole, one half
- 9.2.580 T/R 1: Don't just guess cuz you're gonna have to prove it to me, Erik. This is my question, to, to Meredith, who likes to come up with different number names and Erik sometimes says on the tape, 'I don't know why we have to have more names.' I like to have lots of names, frankly. Um,

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9.2.581 David: Um, wait a minute, um, four twelfths?

9.2.582 T/R 1: Ok, David thinks four twelfths

9.2.583 Erik: One twelfth! One twelfth!

9.2.584 T/R 1: We know it's one twelfth, we agreed it's one twelfth, and you've proved it's one twelfth.

9.2.585 Erik: Four twenty-eighths. I mean, four forty-eighths.

9.2.586 1:1:50 T/R 1: You think four forty-eighths?

9.2.587 Erik: Because the whites would be, the whites would be forty-eighths, and then, and then it takes

9.2.588 David: [interjecting]-I didn't mean- four twelfths I mean four forty-eighths

9.2.589 Erik: [continuing] Four whites to equal up

9.2.590 David: Four twelfths.

9.2.591 Erik: Four forty-eighths.

9.2.592 T/R 1: You mean four forty-eighths.

9.2.593 Erik: I said four forty-eighths.

9.2.594 T/R 1: Meredith? You think that makes sense?

9.2.595 Erik: Four forty-eighths or

9.2.596 Meredith: One twelfth.

9.2.597 Erik: One twelfth.

9.2.598 T/R 1: So we have one twelfth, we have four forty-eighths. Any other names?

9.2.599 Erik: Oh, wait! Oh, yeah! Two, two, two twenty-fourths!

9.2.600 T/R 1: Two twenty-fourths.

9.2.601 Erik: Two twenty fourths

9.2.602 T/R 1: Ok, we have one twelfth, two twenty-fourths, four forty-eighths, anything else? How many different number names and different blocks.

9.2.603 101:27 Erik: Well, does it have to be the same whole?

9.2.604 T/R 1: What do you think?

9.2.605 Meredith: It can also be bigger by, um,

9.2.606 Erik: Two, or it can be thirds, halves, it could be a

9.2.607 T/R 1: What are the green called? What's one green?

9.2.608 Erik: Those are sixteenths.

9.2.609 Meredith: One sixteenth and one forty-eighth.

9.2.610 T/R 1: One sixteenth.

9.2.611 Meredith: And one forty-eighth.

9.2.612 T/R 1: How did you get sixteenths?

9.2.613 Erik: Because there are sixteen all lined up to the answer.

9.2.614 Meredith: One sixteenth

9.2.615 T/R 1: Show me the sixteen.

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- 9.2.616 Erik and Meredith: One two three four five six seven eight nine, ten, eleven, twelve, thirteen, fourteen fifteen, sixteen.
- 9.2.617 1:02:09 T/R 1: Ok, so the green is one sixteenth. But is the difference between three quarters and two thirds a green?
- 9.2.618 Erik: Is the difference between
- 9.2.619 Meredith: A green and one forty-eighth.
- 9.2.620 T/R 1: So how would, what number name would you give for the differences between
- 9.2.621 Erik: Also, the, it also could be it would take two of them to equal up to a brown.
- 9.2.622 T/R 1: Well, these are the things I want you to think about and write about. Ok? I think these are good, good questions that are for you. We're up to seventh grade math already so.
- 9.2.623 Erik: Seventh?
- 9.2.624 T/R 1: So I think you could work it out if you worked hard enough.
- 9.2.625 Meredith: Yeah, but I think if you took one sixteenth and one forty - eighth and you put it up to it, it equals
- 9.2.626 T/R 1: The difference? Oh, so what number name would you give to that, then?
- 9.2.627 1:03:01 Meredith: Uh, one forty eighth [laughs] I don't-
- 9.2.628 T/R 1: Well, think about it. [to class] Ok. I think we have to clean up
- 9.2.629 Class: Ohhh!
- 9.2.630 T/R 1: I know, I'm sorry, I really am, but I hope maybe Mrs. Phillips will let you work on this tomorrow and actually finish writing up what you're doing and describing it for Monday. Is that possible, Mrs. Phillips, that maybe tomorrow they can continue this part of summarizing and write this up?
- 9.2.631 CT: Sure.
- 9.2.632 1:03:45 T/R 1: Oh, good work! You have to think about that! You have to think hard about it. No guessing, you have to be able to convince me, ok?
- 9.2.633 1:03:57 End of class.