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| Line | Time | Speaker | Transcript |
| :---: | :---: | :---: | :---: |
| 1. | 5:32 | T/R 1: | Well, good morning. [students Good morning] What did you do yesterday in math? [students raise hands] Ah, All these people are going to tell me. Amy, |
| 2. |  | Amy: | We did, we figured out the chocolate, we divided chocolate. |
| 3. |  | T/R 1: | Oh. Did you all agree? |
| 4. |  | Students: | Yeah. |
| 5. |  | T/R 1: | You agreed! Was that an easy decision? |
| 6. |  | Andrew: | Yeah. |
| 7. |  | T/R 1: | No discussion, or, or differences? |
| 8. |  | Andrew: | Well, a little |
| 9. |  | T/R 1: | How did that work. |
| 10. |  | Andrew: | Well, we um like divided us into groups, the class into groups and um, and our, in my group, there was like nine people, so each person got like, um one and one ninth. |
| 11. |  | T/R 1: | How did you decide that? How much did you have to start with? |
| 12. |  | Andrew: | We had uh ten pieces. |
| 13. |  | T/R 1: | Ten pieces. I see, how did you do one and one ninth? I'm curious. |
| 14. |  | Andrew: | Well, we um, we said there was nine people, so we had to give a whole piece of candy to each person and then we had one left over so we would have to, and there's nine people, so if we divided it into ninths there would um be enough, for everyone. |
| 15. |  | T/R 1: | Is that hard to do? |
| 16. |  | Andrew: | Yeah, a little. |
| 17. |  | T/R 1: | But you did it? |
| 18. |  | Andrew: | Yeah. |
| 19. |  | T/ R 1: | And you all felt good about it? |
| 20. |  | Graham: | Yeah. |
| 21. |  | T/R 1: | Oh, and you were in that group too, Graham, huh? |
| 22. |  | Graham: | Yeah. |
| 23. |  | T/R 1: | What about another group? What did another group do? You were in a different group? Jessica, what did you do? |
| 24. |  | Jessica: | Well, my group, we like had uh, eight people in our group, so well, we each got one whole piece and then we had two pieces left over so then we divided each of the two pieces into fourths. |

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| 25. |  | T/R 1: | And, so, how, how much did each person get? |
| :--- | :--- | :--- | :--- |
| 26. |  | Jessica: | One and one fourth. |
| 27. | T/ R 1: | You got one and one fourth. Did you all think that was fair, in that <br> group? [mmm hmmm] Did the people in Andrew's group get the same <br> amount as the people in Jessica's group? [no] Who got more, the <br> people in Andrew's group or the people in Jessica's group? Michael? |  |
| 28. |  | Michael: | The people in Jessica's group. |
| 29. | T/R 1: | The people in Jessica's, now, of course I could ask you how much <br> more, you think you could you figure that out? You don't have to tell <br> me that right now. |  |
| 30. |  | Michael: | Yeah |
| 31. | $7: 53$ | Meredith: | Yeah, if we got one ninth and they got one fourth, then um, nine <br> minus four equals five, so they got um one fifth bigger, than we... |
| 32. |  | T/R 1: | Say that again? |
| 33. | Meredith: | See, um, we had, each of us had one and one ninth. |  |
| 34. | T/R 1: | Let's see, let's see, Andrew's group had nine people, right? Each <br> person, |  |
| 35. | Andrew: | Got one and one ninth |  |
| 36. | T/R 1: | And in Jessica's group, eight people and each person got, you said, |  |
| 37. |  | Tessica: | One and one fourth |
| 38. |  | Meredith: | One and one fourth. |
| 39. | T/R 1: | And so, you're telling me, |  |
| 40. | Jessica: | But there was another group. |  |
| 41. | T/R 1: | Maybe we'll hear about the other group and we'll come back to this, <br> but I also didn't want to lose what Meredith said, what Meredith said <br> was the people in Jessica's group got more than the people in <br> Andrew's group. [Meredith laughs] and I, I kind of asked how much <br> more |  |
| 42. | Meredith: | Nine minus four equals five so they got one fifth more. <br> 43. | T/R 1: | | So you're claiming, this is Meredith's claim |
| :--- |
| 44. |

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|  |  |  | group? A group other than Andrew's and Jessica's group? Kimberly? <br> Ahah. How many in your group, Kimberly? |
| :--- | :--- | :--- | :--- |
| 47. |  | Kimberly: | There, we each got one and one fourth. |
| 48. |  | T/R 1: | How many people in your group? |
| 49. | Kimberly: | Eight |  |
| 50. |  | T/R 1: | Eight people? And in your group got |
| 51. |  | Kimberly: | One and one fourth. | | 52. |
| :--- |
| 53. |

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| 63. | Meredith: | Right. |
| :---: | :---: | :---: |
| 64. | T/R 1: | And what number tells you? |
| 65. | Meredith: | Well, um, if they, uh, one fourth, and one rod was like, the one rod, and you had ninths and you had fourths, if you had the fourths they would take |
| 66. | T/R 1: | You're talking about ninths and fourths, is that right? |
| 67. | Meredith: | Yeah. |
| 68. | T/R 1: | You all agree that it's ninths and fourths that's at issue here? And it's not the one piece? So let's focus on the ninth, right, and let's focus on the fourth. So which one you're claiming is bigger? |
| 69. | Students: | The one fourth. |
| 70. | T/R 1: | The one ninth is smaller |
| 71. | Students: | Yeah. |
| 72. | T/R 1: | Did you ever see that symbol, smaller than? [Figure 10-29-02] |
| 73. | Students: | Yeah |
| 74. | T/R 1: | One ninth is smaller than one fourth? Ok? So I'm sorry, Meredith. |
| 75. | Meredith: | And, um, if you take a one rod and you divide it into ninths and fourths, the fourths are going to be larger because they're less. So they're going to be larger. So each person is going to be getting a larger piece. |
| 76. | T/R 1: | Ok, so you've convinced me that if I could imagine a rod that I call one, and I imagine four pieces and I think of one of those pieces, that's going to have what number name? |
| 77. | Meredith: | Fourths. |
| 78. | T/R 1: | And if I take that same rod and imagine nine pieces, one of those pieces will have the number name. |
| 79. | Meredith: | Ninths. |
| 80. | T/R 1: | One ninth. And you could imagine in your head without the rods you're telling me that the one ninth is, that the one fourth is |
| 81. | Meredith: | Bigger than |
| 82. | T/R 1: | Bigger than the one ninth, or the one ninth is smaller than the one fourth. The question I'm asking is the difference one fifth? Now, could you imagine the fifth rod, what that looks like? |
| 83. | Meredith: | Um, I think it would be the yellow rod, I'm not sure, I think it was the yellow rod that was the fifth. |
| 84. | T/R 1: | Whatever you're thinking, but you could imagine a fifth, you could imagine a fourth, you could imagine a ninth, and do you imagine in your head, my question, do you imagine in your head that the, if you'd |

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|  |  |  | compare the one fourth rod and the one ninth rod, the difference would be the one fifth rod, do you think that, does that make sense to you, as you're imagining this in your head? |
| :---: | :---: | :---: | :---: |
| 85. |  | Meredith: | Ummm, if you put the four and the five together it would equal up to the ninth rod. |
| 86. |  | T/R 1: | You think so? [mmm] I think we ought to get out the rods. |
| 87. |  | CT: | Yeah. |
| 88. | 15:09 | T/R 1: | I think we ought to get out the rods, what do you think? How many of you want to work on this? How many of you want to know how much more the people in Andrew's and Je- uh, Andrew's group, uh Jessica's group and Kimberly's group got than the people in Andrew's group. [Students raise hands, Dr. Landis enters with rods] Can somebody tell Dr. Landis the problem because she doesn't know any of the story of any of what happened and how this all came to be, could someone be so kind as to tell Dr. Landis the whole story? Kimberly do you want to give it a try? Dr. Landis? Do you want to hear what's going on? |
| 89. |  | Dr. Landis: | I do want to hear it, yes! |
| 90. | 15:46 | Jessica: | It's not, it's not going to be an orange |
| 91. |  | Andrew: | I'm going to make a whole model |
| 92. |  | Jessica: | It's a yellow, that's a fifth, you don't have to make a whole model. |
| 93. |  | Andrew: | To figure it out you do. Here's fourths and ninths would be one two three [Andrew's model is an orange and red train, and four light green rods, Figure 10-29-03] |
| 94. |  | Jessica: | Well that's ninths, cuz it's sixths [Jessica's model is a yellow rod and four white rods, Figure 10-29-04] |
| 95. |  | Andrew: | What are you doing? |
| 96. |  | Jessica: | Nothing. [Andrew lines up six red rods, Figure 10-29-05]. This one doesn't show ninths |
| 97. |  | Andrew: | Gotta make it bigger. Orange and a purple |
| 98. |  | Jessica: | You do? You have to make it bigger if it doesn't work? Now I need the green. |
| 99. |  | Andrew: | I need the purples. |
| 100. |  | Jessica: | I need the purples. [Jessica makes an orange and purple train, first places green rods, then removes them, Figure 10-29-06] |
| 101. |  | Andrew: | I have to make even bigger! |
| 102. |  | Jessica: | Wait, first you make it small |
| 103. |  | Andrew: | Let's try two more bigger. How about the brown, that's good |

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| 104. |  | Jessica: | Look you can make it like this. And then you have it, look. Andrew. |
| :---: | :--- | :--- | :--- |
| 105. |  | Andrew: | I don't want to hear it. |
| 106. | Jessica: | Well, it's the same thing as the greens, I think it is. Yeah it's the same <br> thing. Could I have another box? Ok. |  |
| 107. |  | Andrew: | One, two, three, four, five, six, seven, eight. [Andrew has built an <br> orange rod next do a dark green rod with eight red rods beside it, <br> Figure 10-29-07] No! Ahh. I'm gonna die! I am really, really, really, <br> really gonna die. You know how far I've gotten up to? |
| 108. |  | Jessica: | Look at this purple, it looks red. No it doesn't. |
| 109. | $19: 15$ | Andrew: | Make it go smaller. We need to do something smaller |
| 110. |  | Jessica: | This is working, I know what I'm going to do. Like this is more than <br> nine, oh reds. |
| 111. |  | Andrew: | I can't find the fourths. Maybe these are fourths. |
| 112. | Jessica: | Five, six, seven, eighths, ninths, didn't work. |  |
| 113. | Andrew: | I have ninths, I have thirds. If there's thirds, there has to be fourths, but <br> I cannot find fourths. [Andrew has an orange next to a brown, nine <br> red rods, and three dark green rods, Figure 10-29-08] |  |
| 114. |  | Jessica: | These don't work. There's a million purples. Oh, you just have to add a <br> red. |
| 115. |  | Andrew: | I'm just doing two oranges and a brown. I've had it! |
| 116. |  | Jessica: | You're not going to get, oh yeah, you are. |
| 117. |  | Andrew: | I want fourths. Fourths is going to be the browns. One, two |
| 118. |  | Jessica: | Fourths. How do you come up with fourths? |

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| 131. |  | Andrew: | Oh, good, give me those two in your hand |
| :---: | :---: | :---: | :---: |
| 132. |  | Jessica: | I need 'em I'm trying something |
| 133. |  | Andrew: | You don't need 'em |
| 134. |  | Jessica: | Ok, one. I'm trying to see something. |
| 135. |  | Andrew: | What are they? Come on, I'll find out for you. Just, fine, have it your way. |
| 136. |  | Jessica: | If I put reds that's fourteenths. |
| 137. |  | Andrew: | Do I care? Sevenths, one two three four five six seven. And two more of these, is four of these, and a half, a half, a half |
| 138. |  | Jessica: | One two three, four, fifths, sixths |
| 139. | 23:19 | T/R 2: | How's it going? I'm sort of watching what you're doing. What have you tried here? |
| 140. |  | Andrew: | Well we've tried |
| 141. |  | Jessica: | Eighths, oh I think I've |
| 142. |  | Andrew: | like um |
| 143. |  | Jessica: | got it. |
| 144. |  | Andrew: | We've tried making models |
| 145. |  | Jessica: | We're trying to make one model that has |
| 146. |  | Andrew: | Fourths and |
| 147. |  | Jessica: | And ninths |
| 148. |  | Andrew: | Ninths |
| 149. |  | T/R 2: | And what have you tried? What are some of the things you've tried to call one? |
| 150. |  | Andrew: | Well we tried to call this one, [orange and red] this [orange and purple, |
| 151. |  | Jessica: | I think I've got it. |
| 152. |  | Andrew: | this, and now we're working on this. |
| 153. |  | T/R 2: | Oh, that's interesting. Ok. |
| 154. |  | Jessica: | I got, I th- I just got, I thought I got ninths here, the light green, but then I counted one two three four five six seven eighths ninths, and then I have that little space. [Jessica has two orange rods and a brown rod next to four black rods and nine light green rods, Figure 10-29-10] |
| 155. |  | T/R 2: | Something hanging over there, ok. |
| 156. |  | Andrew: | So then it's going to be impossible. So then you need |
| 157. |  | T/R 2: | So you have a plan? What are you going to try next? |
| 158. |  | Jessica: | Oh, purples. No but I did. |
| 159. |  | Andrew: | Cut this [the brown rod that is part of the two orange and one brown train] in half this is a purple |

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| 160. |  | Jessica: |
| :--- | :--- | :--- |
| 161. |  | I can add |
| 162. |  | Jessica: | So let's try a purple | And then put browns there maybe, wait, yes. It's working. Then I |
| :--- |
| could put browns there. |$.$| Ok, I'll let you experiment some more. Let me know if you come up |
| :--- |
| with one that works, ok? |.

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| 191. | Both: | We're trying to figure out |
| :--- | :--- | :--- |
| 192. | Jessica: | We're trying to figure out a problem that has both of them in it |
| 193. | T/R 1: | That has both of what in it? |
| 194. | Jessica: | Like, um, both one ninth and one fourth. |
| 195. | T/R 1: | Very good. |
| 196. | Jessica: | And we got one fourth |
| 197. | T/R 1: | Ok |
| 198. | Jessica: | We got one fifth and we still, we need one ninth. And I was just trying <br> to count that as one, then one, and one. |
| 199. | T/R 1: | Ok, so that's what you're working on. Ok that's a good thing to work <br> on |
| 200. |  | Jessica: | And one and one, but that doesn't work, that's this again. | T/R 1: |
| :--- |
| 201. |
| 202. |

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| 218. |  | Andrew: | Like two browns are the fourths, and I remember that I put two of these together, they would be the thirds |
| :---: | :---: | :---: | :---: |
| 219. |  | Dr. Landis: | Right |
| 220. |  | Andrew: | So I have thirds but I don't need thirds |
| 221. |  | Dr. Landis: | Uh huh |
| 222. |  | Andrew: | These two are one fourth |
| 223. |  | Dr. Landis: | Oh I see |
| 224. |  | Andrew: | So how many fourths do you have there? |
| 225. |  | Andrew: | One two three, I need one more. Two more |
| 226. |  | Jessica: | We need a lot more browns |
| 227. |  | Dr. Landis: | Do you think maybe, you're running out of rods, do you think if you work together to build one model that would help? |
| 228. |  | Jessica: | Yeah 'cause we're running out, I need a lot more. |
| 229. |  | Andrew: | I need |
| 230. |  | Jessica: | We have like three boxes |
| 231. |  | Dr. Landis: | Oh, you have another box? Oh. But it doesn't have the colors? Do you want another box to work separately or do you want to build the same model? |
| 232. |  | Jessica: | Well, we're building the same one |
| 233. |  | Dr. Landis: | Ok, I mean do you want to work together to build one model or do you want me to get you some more rods so you can get your own? |
| 234. |  | Jessica: | Oh there's bags of rods over there. |
| 235. |  | Dr. Landis: | There are more? Ok. |
| 236. | 31:18 | Jessica: | [Comes back with rods] I got one |
| 237. |  | Andrew: | Oh my, I have no browns left. I found a brown! It has beads in it. |
| 238. |  | Jessica: | I know |
| 239. |  | Andrew: | You could have just got a bag. |
| 240. |  | Jessica: | Well this has a lot, the others didn't have any browns. |
| 241. |  | Andrew: | These were the fourths. Done with that! Done done done! |
| 242. |  | Andrew: | Yeah I don't need any more. |
| 243. |  | Dr. Landis: | You have enough, ok? |
| 244. |  | Andrew: | The browns were the thirds. |
| 245. |  | Jessica: | Oh the browns were the thirds. |

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| 246. |  | Dr. <br> Landis: | Do you have enough of what you need to? |
| :---: | :---: | :---: | :---: |
| 247. |  | Jessica: | Um, yes. |
| 248. |  | Dr. Landis: | Ok. |
| 249. |  | Andrew: | Now I need greens. |
| 250. | 32:43 | Dr. <br> Landis: | You said you needed some more of these colors |
| 251. |  | Andrew: | Thank you |
| 252. |  | Dr. Landis: | I'll leave it here. |
| 253. |  | Jessica: | Ok. Andrew, can you put this on the other side of the desk. |
| 254. |  | Dr. Landis: | What you can do is you can put this in here and that way you won't have so many containers. How's that? You want to get rid of this? |
| 255. |  | Jessica: | Um yeah, we don't need one. |
| 256. |  | Andrew: | Green in half [inaudible] |
| 257. |  | Jessica: | It didn't work, purples, four browns, three browns and a purple it was. |
| 258. |  | Andrew: | Three browns and a purple? It was two purple |
| 259. |  | Jessica: | Oh yeah, something and two purples. Like three oranges and two purples it was |
| 260. |  | Andrew: | Two purples, two purples equals one brown. And that's not equaling up. |
| 261. |  | Jessica: | Yeah but that is only three oranges. |
| 262. |  | Andrew: | Oh! |
| 263. |  | Jessica: | Does that make sense? |
| 264. |  | Andrew: | That's why! You took it off. |
| 265. |  | Jessica: | That was mine |
| 266. |  | Andrew: | Hey that was mine. |
| 267. |  | Jessica: | Here's another one. |
| 268. |  | Andrew: | Oh. Let's move it down this way. |
| 269. |  | Jessica: | Purples... it was four and two purples, right? |
| 270. |  | Andrew: | Four and one brown |
| 271. |  | Jessica: | Or two purples |
| 272. |  | Andrew: | Or two purples. Just making it look smaller. This doesn't work anyway. It works. |
| 273. |  | Jessica: | I have no clue. |
| 274. |  | Andrew: | Alright, we needed sixths, fifths. |
| 275. |  | Jessica: | Fifths. Um, one two three fourths, um now it's browns. |

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| 276. |  | Andrew: | Why would browns be fifths? |
| :---: | :---: | :---: | :---: |
| 277. |  | Jessica: | I don't know. |
| 278. |  | Andrew: | Regular browns? |
| 279. |  | Jessica: | What are browns gonna be? |
| 280. |  | Andrew: | Maybe, maybe. |
| 281. |  | Jessica: | One |
| 282. |  | Andrew: | Hey you're taking out of my bin. One, two, three four |
| 283. |  | Jessica: | Ok, browns are thirds. |
| 284. |  | Andrew: | Five. No they're not. |
| 285. |  | Jessica: | Yeah they are. |
| 286. |  | Andrew: | I'm not counting by two. Count by ones. |
| 287. |  | Jessica: | Six |
| 288. |  | Andrew: | Count by ones. |
| 289. |  | Jessica: | One two three four five six seven eight |
| 290. |  | Andrew: | Ones |
| 291. |  | Jessica: | I am. |
| 292. |  | Andrew: | One two three four five |
| 293. |  | Jessica: | Six. Ok, so |
| 294. |  | Andrew: | I can't figure this out. |
| 295. |  | Jessica: | One two three four five six |
| 296. |  | Andrew: | We did have sixths |
| 297. |  | Jessica: | Seven eighths, |
| 298. |  | Andrew: | We did have twelfths |
| 299. |  | Jessica: | One two three four five six. Because we were counting by two as one. |
| 300. |  | Andrew: | Did we have tenths? |
| 301. |  | Dr. Davis: | Carolyn, you want to bring the mike? |
| 302. |  | Andrew: | Did we have tenths. |
| 303. |  | Jessica: | Tenths? Yes reds. |
| 304. |  | Andrew: | Reds were tenths. |
| 305. |  | Jessica: | No green. No purples. Purples [mike moves to James] |
| 306. |  | : | [most of this conversation is inaudible] |
| 307. | 38:00 | James: | I took the ninths [purples] and yellows So I worked out like this. [inaudible] is bigger than one ninth. |
| 308. |  | Dr. Davis: | Oh, so what's the answer? |
| 309. |  | James: | Five whites equal up to a blue and the ninth is the purple and the blue |
| 310. |  | Dr. Davis: | So the blue is one fourth and the purple is one ninth? |
| 311. |  | James: | Yeah. |
| 312. |  | Dr. Davis: | What's the white rod? [inaudible] What you call this? |

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\(\left.$$
\begin{array}{|c|l|l|l|}\hline 313 . & & \text { James: } & \text { Uh, one thirty-sixth. } \\
\hline 314 . & & \begin{array}{l}\text { Dr. } \\
\text { Landis: }\end{array} & \text { One thirty-sixth, he said. One thirty-sixth. } \\
\hline 315 . & & \text { Dr. Davis: } & \text { Can you explain that again? } \\
\hline 316 . & & \text { Janother mike is brought over] } \\
\hline 317 . & 39: 50 & \begin{array}{l}\text { Ok, first I tried nine yellows, and I tried to equal up the orange with } \\
\text { the nine yellows, four oranges to equal the nine yellows, and the } \\
\text { oranges were too small, so then I put nine purples right here, and then } \\
\text { I put this [holds up orange rod] at a lower level in size, and then I took } \\
\text { blues, and that equaled up to the nine purples. Then I just had to make } \\
\text { a whole and my whole right now is three oranges and a dark green. } \\
\text { [Figure 10-29-14] }\end{array} \\
\hline 318 . & & \text { Dr. Davis: } & \text { Alright, that's very nice. And so the white rod is? } \\
\hline 319 . & & \text { James: } & \text { One, uh, thirty-sixths. They equal five } \\
\hline 320 . & & \text { Dr. Davis: } & \begin{array}{l}\text { And what did you do over here? [pointing to model with a blue rod } \\
\text { next to five white rods and a purple rod] }\end{array} \\
\hline 321 . & & \text { James: } & \begin{array}{l}\text { Well, I, I just think that the blue is bigger than the purple by one fifth } \\
\text { cuz it takes five whites to equal up to the blue, the one fourth. }\end{array} \\
\hline 322 . & & \text { James: } & \begin{array}{l}\text { Now, let me get this straight. The purple rod is, what name do you } \\
\text { give to that? }\end{array} \\
\hline 323 . & & \text { One ninth. } \\
\hline 324 . & & \text { James: } & \text { Dravis: }\end{array}
$$ \begin{array}{l}One ninth, I understand that because nine of them are as long as your \\

[inaudible]\end{array}\right]\)| Uh huh. |
| :--- |
| 325. |

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| 337. |  | James: | Um, how much bigger is one fourth than one ninth? |
| :---: | :---: | :---: | :---: |
| 338. |  | Dr. Davis: | Yeah. And your answer is? |
| 339. |  | James: | Five thirty-sixths. |
| 340. |  | Dr. Davis: | I think that's gorgeous. |
| 341. |  | Dr. <br> Landis: | Yeah, I'm impressed too. |
| 342. |  | T/R 1: | Can you write that up on an overhead for me and draw a picture, James? |
| 343. |  | James: | Uh, yeah. |
| 344. |  | Dr. Davis: | Thanks. |
| 345. | 42:35 | Andrew: | Yes, it fits |
| 346. |  | Jessica: | But how do you make ninths? With um |
| 347. |  | Andrew: | Easy, you get a four. Anything but ninths. Hmm [Andrew's model is two orange rods, with four yellow rods beside it] ninth would be |
| 348. |  | Jessica: | The fifth would be green, right? |
| 349. |  | Andrew: | Yes it is. [Andrew places down light green rods, Figure 10-29-15] |
| 350. |  | Jessica: | One two three four five six seven. |
| 351. |  | Andrew: | We need something, how about red? |
| 352. | 43:53 |  | [camera moves to Kelly's desk with a model identical to James' inaudible] |
| 353. |  | Kelly: | We know what it is [some talk about copying] |
| 354. |  | Jessica: | It's for the ninths and the fifths |
| 355. |  | Erik: | One two three four five six |
| 356. |  | Michael: | One two three four five six seven eight nine. |
| 357. |  | Erik: | Wait, one two, I don't like you. One two three four five six seven eight nine one two three four not fair |
| 358. |  | Michael: | We almost solved that, me and Erik were right at the edge of it, and then we sort of went into space with another idea. |
| 359. |  | Erik: | [some nasty comments] |
| 360. |  | Meredith: | Do you have any one rods? |
| 361. |  | Graham: | Yes. |
| 362. |  | Meredith: | If you called them, if you made a new model and made them halfs, and then |
| 363. |  | Michael: | Graham you know, can I just use |
| 364. |  | Graham: | We don't need these, we don't need these |
| 365. | 48:41 | T/R 1: | How is this model related if at all to these models? |
| 366. |  | Michael: | I don't know... Oh! |
| 367. |  | Erik: | Well they don't have fifths, and they don't have this. |

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| 368. |  | T/R 1: | No, they don't. |
| :---: | :--- | :--- | :--- |
| 369. | Michael: | They have ninths - like that! One two three four five six seven eight <br> nine. |  |
| 370. |  | T/R 1: | They're comparing ninths and fourths, Meredith, why do they need <br> fifths. Your theory is they need fifths. Now they're comparing ninths, <br> this is fourths, right? [Lays down blue rod] And this is ninths, is that <br> correct? [Lays down purple rod] |
| 371. |  | Graham: | Yeah [Figure 10-29-16] |
| 372. | T/R 1: | You're comparing fourths and ninths and it's this, ok? [Graham hands <br> teacher the yellow rod, and she shows that the yellow and purple are <br> the same length as the blue rod] |  |
| 373. |  | Meredith: | It's my method |$|$| T/R 1: |
| :--- |
| 374. |
| 375. |

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| 394. |  | T/R 1: | How many? What's the difference? |
| :---: | :---: | :---: | :---: |
| 395. |  | Graham: | Well there are thirty-six. |
| 396. |  | T/R 1: | There are thirty-six of these? |
| 397. |  | Graham: | Yeah, the whites. |
| 398. |  | T/R 1: | And what's the difference between the two? How many of the thirtysixths? |
| 399. |  | Graham: | Five. |
| 400. |  | T/R 1: | So the difference between one ninth and one quarter is how much? |
| 401. |  | Graham: | Five |
| 402. |  | Kimberly: | Thirty-sixths. |
| 403. |  | T/R 1: | Five thirty-sixths. |
| 404. |  | Meredith: | And one fifth. |
| 405. |  | T/R 1: | Well, where's the one fifth? |
| 406. |  | Meredith: | Well, if you had one |
| 407. |  | Kelly: | There's no one fifth. |
| 408. |  | T/R 1: | Do you think that, do you think this is five thirty-sixths, if you could imagine one fifth in here, |
| 409. |  | Meredith: | Yeah, uh huh. |
| 410. |  | T/R 1: | Right? You could imagine one fourth, it's the blue, right? Is this one fifth? |
| 411. |  | Meredith: | Uh... |
| 412. |  | T/R 1: | If it were one fifth. |
| 413. |  | Graham: | It would be too big. |
| 414. |  | T/R 1: | [places five yellow rods down, Figure 10-29-18] Would that would be one fifth? Is that big enough to be one fifth? |
| 415. |  | Kelly: | I don't think it's one fifth. |
| 416. |  | Meredith: | Well it does have five here [places a yellow rod on the five white rods, Figure 10-29-13] |
| 417. |  | T/R 1: | It's this length but this has the number name, what, the yellow has what number name? |
| 418. |  | Students: | Five thirty-sixths |
| 419. |  | T/R 1: | Five thirty-sixths. Not one fifth, right? |
| 420. |  | Meredith: | Uh huh. |
| 421. | 53:33 | T/R 1: | Think about what is causing the difficulty, ok, Meredith? [to class] Ok, is this a good time maybe to pull together for a few minutes and do some sharing? [no] Is this a good time? [to Kelly] Keep your model here. [to class] Ok. Is it possible, can, can I have your attention |

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|  |  |  | for a minute, we have a little bit of extra time thanks to Dr. Landis, uh, she's given us a little extended time, but we have some interesting ideas here and I think it's really important to share our ideas, I see some wonderful models another model here, right, with, um, Mark and Audra, right? You have another model. I guess, um, I was very interested in listening to your ideas as I walked around and I heard um our, does anyone, did anyone change their mind what they thought the difference between, uh, one quarter and a ninth were? Did anybody change their mind? Some of you changed your minds? How many of you still aren't sure about that difference [some students raise their hands]. Ok, so, so we had a theory, let's call it Meredith's theory, but she may have changed her mind she may not have, but Meredith's theory seems to suggest that if you wanted to find the difference between one fourth and one ninth that it's one fifth. That was the theory that we were testing, right? Now, if you used that same theory and I asked you what the difference was between one quarter and a third, and you applied that theory, what would you have said the difference was between a quarter and a third? |
| :---: | :---: | :---: | :---: |
| 422. |  | Meredith: | A quarter and a third? |
| 423. |  | T/R 1: | Using that same theory. |
| 424. |  | Meredith: | A quarter and a third would be, well, how big would the third be. |
| 425. |  | T/R 1: | Ok, well one of the gentlemen here who have built the models up here, can you all kind of listen for a minute to what Michael and Erik and um James have built |
| 426. |  | Students: | James? |
| 427. |  | T/R 1: | I'm sorry, not James, David. |
| 428. | 56:12 | Michael: | Um, uh, well, what me and Erik, me and Erik started building models like these [Figure 10-29-20] to try and help us figure out how to one fourth and one ninth, and Dr. Ma- and um, and then we were on the edge of trying to find it out and then we had another idea we started just we lost the idea of that was that we had before and |
| 429. |  | T/R 1: | Do you want to tell us what that idea was? |
| 430. |  | Michael: | Well, that idea was, try to get, try to um find the number and divide, and, um, divide it and see if it equals nine, then you've got a ninth, but we found that every single one that we tried there wasn't a fourth if there was a ninth, and if there was fourth there wasn't a ninth. So, um, we, we, um, we decided to try a new idea it turns out when we, uh, when we tried the new idea, the first time we tried it we were wrong. |
| 431. |  | T/R 1: | What was that new idea? |

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| 432. |  | Michael: | Well, I don't really remember what we were thinking. |
| :---: | :---: | :---: | :---: |
| 433. |  | T/R 1: | Was it the odd and even? |
| 434. |  | Michael: | Yeah, I think so, yeah, what I also figured, um, is that you, it's so hard, like if you had you had to make a model with one fourth and one eighth in it, we could make a ton of them, but it's hard to make a model that has an odd number, which is one ninth, and a even number, which is one fourth. So I figured that that was really hard and there was only like two models or so of it and it was really hard to find you would have to make trains or something like that. |
| 435. |  | T/R 1: | Ok, so where did that leave you. You told me there couldn't be any models when you had an odd and even. |
| 436. |  | Michael: | I know. But then we figured that it had to be, because there was no other way to do it. |
| 437. |  | T/R 1: | But you built two models here and you're comparing fractions where, you have an odd and even number on |
| 438. |  | Michael: | Well, I didn't really, I was just building, I was just trying to get an idea from these old models and I didn't get one, but I guess Dr. Maher did, so she wanted us to come up and say what we were thinking, I was just trying to get an idea from it. |
| 439. |  | T/R 1: | When you compare this top one, what numbers were you comparing when you built this model here? [Continuing figure 10-29-20] |
| 440. |  | Michael: | One third and one fourth. |
| 441. |  | T/R 1: | And what did you find? |
| 442. |  | Michael: | We found that it worked. |
| 443. |  | T/R 1: | What worked? |
| 444. |  | Michael: | That an odd and an even can go into a whole. |
| 445. |  | T/R 1: | So, you mean you compared a quarter and a third, what did you find to be that difference? |
| 446. |  | Michael: | The difference would be, the difference would be one twelfth. But in this model with the half and the third it would be one sixth. |
| 447. |  | T/R 1: | Ok, so you could do that. Ok, um, alright, let's see, now James did James has some idea here let's here what James says and we all know that Graham and, why don't you sit down? Thank you very much, gentlemen. And let's, let's hear what James' idea is and then we'll hear if Graham and Kelly agree. Where did Graham go? |
| 448. |  | James: | [at OHP] can I take this off? |
| 449. | 59:35 | T/R 1: | Yeah, sure. |
| 450. |  | James: | [James put an overhead transparency on OHP, Figure 10-29-21] Well, |

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|  |  |  |
| :--- | :--- | :--- |

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|  |  |  | the ninth and the quarter? |
| :---: | :---: | :---: | :---: |
| 471. |  | Jackie: | Five thirty-sixths. |
| 472. | 1:03:08 | T/R 1: | How many of you got five thirty-sixths? I see. I see. Ok, what do you think? So, so you can actually see, what makes this problem so hard? What do you think makes it so hard? |
| 473. |  | Kimberly: | The odd number and the even number. |
| 474. |  | T/R 1: | Pardon? |
| 475. |  | Kimberly: | The odd number and the even number. |
| 476. |  | T/R 1: | The odd and the even number? What about that makes it hard? You have a four and a nine. |
| 477. |  | Kimberly: | Because it's harder to make a model when you have an even number for one and an odd for the other. |
| 478. |  | T/R 1: | Ok, now have you learned anything on the models that you've seen today that might help you get some ideas for how to pick that number? If you remember that Erik and Michael when they compared a half and a third, what was your difference? |
| 479. |  | Michael: | A half and a third? |
| 480. |  | Erik: | A half and a third was |
| 481. |  | Michael: | Was one sixth. |
| 482. |  | T/R 1: | When you compared a half and a third it was one sixth. And when you compared a third and a quarter? |
| 483. |  | Erik: | It was, it was, one one twelfth. |
| 484. |  | T/R 1: | It was one twelfth. And when you compared a quarter and a ninth? |
| 485. |  | Michael: | A quarter and a ninth? |
| 486. |  | T/R 1: | One fourth and one ninth? |
| 487. |  | Michael: | Oh. |
| 488. |  | T/R 1: | It became, who did it here? You did it here, Erin and Beth you got five thirty-sixths. |
| 489. |  | Michael: | Oh, it sort of went up by six I guess. |
| 490. | 1:04:40 | T/R 1: | It's something to think about, isn't it? It's something to think about, right? Well we have here, thank you very much, and Kelly and Graham and all of those wonderful models, I'm going to keep this, that's lovely, thank you. How many of you believe the difference is five thirty-sixths, raise your hands. If you don't believe it, if you need to walk over to these models before we put them aside and see what they've done. When, we compared one half and a third, we got one sixth. When we compared a third and a quarter, right? We got one twelfth. When we compared a quarter and a ninth we got five thirty- |

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|  |  |  | sixths. [Writes on transparency: $1 / 2-1 / 3=1 / 6,1 / 3-1 / 4=1 / 12,1 / 4-$ <br> $1 / 9=5 / 36$, Figure 10-29-22.] Is there anything in these numbers that <br> relate to the model you built? That's my question. Well we can think <br> about that. I think we have to stop. If you haven't built the model, I <br> really think we have enough people here, we have Kelly and Graham, <br> we have the table in the back, what do you think? Ok, so we can think <br> about them. But, I'm wondering if there's anything that might give you <br> a clue to building your models in the future. Maybe you ought to try to <br> build some more and study these a little bit. It's something to think <br> about, huh? Ok, well I'm going to see you on Monday, [good!] and we <br> can talk some more. Thank you very much and thank you for staying <br> longer, I appreciate, Mrs. Phillips, the extra time. A really good job. |
| :--- | :--- | :--- | :--- |
| 491. | $1: 06: 33$ | end of class |  |

