## Transcript:

| Line | Time | Speaker | Transcription |
| :--- | :--- | :--- | :--- |
| 1783 | $0: 30$ | R2 | Jerel and Chris, how are you guys doing? |
| 1784 |  | C\&J | Good. |
| 1785 |  | R2 | Yeah, well thank you for coming down here. 'Cause I told you |
| 1786 |  |  | there are some things, uh, that I heard you talk about, some ideas |
| 1787 |  |  | that you have that I'm really interested in hearing more about. |
| 1788 |  |  | And since it's so noisy down at the other end of the room, and the |
| 1789 |  |  | hall, I thought we would, uh, chat here. Okay? So last week |
| 1790 |  |  | Thursday we started working on some dice games. |
| 1791 |  | C\&J | Um humh. [in unison] |
| 1792 |  | R2 | And do you remember the very first game that we worked on? |
| 1793 |  | C\&J | Yeah. [in unison] |
| 1794 |  | Jerel | The one that was unfair. |
| 1795 |  | R2 | The one that was unfair. Could you tell me about that first game? |
| 1796 |  |  | What was the rules of that first game? |
| 1797 |  | Jerel | The rules was that Player A got, uh, numbers 2 . . [scratches his |
| 1798 |  |  | neck, then reaches for paper]. Ah, I can look at this one, it'll tell. |
| 1799 |  |  | Player A got 2, 3,... |
| 1800 |  | Chris | No, that's the one we did that today. |
| 1801 |  | R4 | That's the second game. Do you want to see the rules of the first |
| 1802 |  |  | one? [To Chris]: Do you remember anything about the first one? |
| 1803 |  | Chris | [Shakes his head no.] Nope. |
| 1804 |  | R2 | Okay. [Gives paper to Jerel.] |
| 1805 |  | Jerel | I remember that Player A had, uh, [pause - looking at and pointing |
| 1806 |  |  | on the paper], I remember that Player A had 1, 2, 3, or 4. And |
| 1807 |  |  | Player, if it landed on one of them A gets one point and Player B |
| 1808 |  |  | gets zero. And if the die had landed on 5 or 6, Player B gets one |
| 1809 |  |  | point. And then from there we knew it was unfair because Player |
| 1810 |  |  | A had more choices than Player B can. And Player B only had |
| 1811 |  |  | two. |
| 1812 | $2: 02$ | R2 | So you think that your, you think that that game is unfair because |
| 1813 |  |  | Player A has more choices than Player B? |
| 1814 |  | Chris | Yep. |
| 1815 |  | R2 | Uh huh. And, um, would it matter, you're saying more choices or |
| 1816 |  |  | because of the numbers that they? |
| 1817 |  | Chris | They got more choices. |
| 1818 |  | R2 | They had more choices, okay. |
| 1819 | $2: 20$ | Jerel | It's a higher percentage of, it 1,2, it landed on 1, 2, 3, or 4 than 5 |
| 1820 |  |  | or 6. |
| 1821 |  | R2 | Uh huh. When you say it's a higher percentage, you know what |
| 1822 |  |  | percentage, or do you have any idea? |
| 1823 |  | Chris | [Shakes head no.] |
| 1824 |  | Jerel | Chance. |


| 1825 |  | R2 | Chance, uh? Do you have any idea how likely it is for Player A to |
| :---: | :---: | :---: | :---: |
| 1826 |  |  | get a point than Player B? |
| 1827 |  | C\&J | [Nod their heads to indicate yes.] |
| 1828 |  | Jerel | Uh huh. |
| 1829 |  | R2 | Yeah? What can you say about that? |
| 1830 |  | C\&J | [In unison] That ... [Jerel indicates that Chris should speak.] |
| 1831 |  | Chris | The probability of getting is 4 out of 6, 'cause there's 6 numbers |
| 1832 |  |  | on the dice and he has 4 chances of getting it. |
| 1833 |  | R2 | Um humh. And did you guys play the game? |
| 1834 |  | C\&J | Yeah. |
| 1835 |  | R2 | Uh huh. And what happened? Tell me about what happened when |
| 1836 |  |  | you played the game. |
| 1837 |  | Jerel | [grabs paper] All right this was the first game. I beat Chris 10 to 2 . |
| 1838 |  | R2 | And you were ... |
| 1839 |  | C\&J | Player A. |
| 1840 |  | R2 | Player A. You were Player A. On the first game you received 10 |
| 1841 |  |  | points and Chris received 2. |
| 1842 |  | C\&J | [Nod in agreement] |
| 1843 |  | R2 | Okay. Did you play the game anymore? |
| 1844 |  | Jerel | Yeah. We played it one more time to see if it, we changed, we |
| 1845 |  |  | changed ... |
| 1846 |  | Chris | sides rules. |
| 1847 |  | Jerel | Chris became Player B and I became, I mean Chris became Player |
| 1848 |  |  | A and I became Player B. And he beat me 5 to 6. I mean 10 to 6. |
| 1849 |  | R2 | 10 to 6. |
| 1850 |  | Chris | Um humh, 'cause we had to change the rules. We put that Player |
| 1851 |  |  | A gets 3 choices 1, 2, and 3, and Player B got 4, 5, and 6. |
| 1852 |  | R2 | Oh, I see. So that's when, when you decided to change the rules of |
| 1853 |  |  | the game to make it, why did you change the rules? |
| 1854 | 3:45 | C\&J | [In unison] So it could be fair. |
| 1855 |  | R2 | So you changed it so it could be fair. |
| 1856 |  | C\&J | Uh huh. |
| 1857 |  | Chris | 'Cause, uh, the first game, since it was 10 to 2 , that was a kill by 8 |
| 1858 |  |  | points, but in the second game it was only a kill by 4 points. |
| 1859 |  | R2 | Okay. Well, let's go back to the first game for a minute. Um, do |
| 1860 |  |  | you think that if you played the first game, right, where Player A |
| 1861 |  |  | receives a point if it receives, if it rolls $1,2,3$, or 4, and Player B |
| 1862 |  |  | receives a point if the dice rolls, if the die rolls 5 or 6, do you think |
| 1863 |  |  | that that game, if you played it 6 times, would it be ... who, who |
| 1864 |  |  | do you think might win? |
| 1865 |  | Chris | Player A. |
| 1866 |  | Jerel | Player B. Player A |
| 1867 |  | R2 | You still think Player A might win. |
| 1868 |  | Jerel | [Nods in agreement.] |
| 1869 |  | R2 | All 6 times? Or just once? |


| 1870 |  | Jerel | All 6 times. |
| :---: | :---: | :---: | :---: |
| 1871 |  | Chris | Almost all 6 times. |
| 1872 |  | R2 | Yeah? Suppose you were to play the game 60 times. |
| 1873 |  | Jerel | Player A would still win. |
| 1874 |  | R2 | Yeah? Do you have ... |
| 1875 |  | Chris | Most of the games. |
| 1876 |  | R2 | Most of the games? When you say most ... |
| 1877 |  | Jerel | 59 out of 60, yeah. |
| 1878 |  | R2 | 59 out of the 60 games Player A? What about 100 times? |
| 1879 |  | C\&J | [smile] |
| 1880 |  | Jerel | 99 out of 100 |
| 1881 |  | R2 | Yes. 99 out of 100. So it seems like Player B's chances goes |
| 1882 |  |  | down the longer, the more that you play the game. Is that right? Is |
| 1883 |  |  | that what you're saying? |
| 1884 |  | C\&J | Um humh. Yep. |
| 1885 |  | R2 | What about your fair game? Tell me about your fair game. What |
| 1886 |  |  | were the rules? |
| 1887 | 5:12 | Jerel | Uh, that ... |
| 1888 |  | Chris | The rules were that um Player A, if Player A rolled a 1, 2, or 3, it |
| 1889 |  |  | would got a point, it would get a point, and Player B woulda got |
| 1890 |  |  | zero. But if Player B rolled a 4, 5 , or 6 , it woulda got a point. |
| 1891 |  | R2 | I see. So why is that fair? |
| 1892 |  | Jerel | Because, they, it's a 50-50, it's a 50-50 chance of Player A or |
| 1893 |  |  | Player B winning. |
| 1894 |  | R2 | What do ya mean 50, you mean if you played a hundred times, |
| 1895 |  |  | what would you expect to happen? |
| 1896 |  | Chris | Probably 50 each. |
| 1897 |  | R2 | They would each win 50 times? |
| 1898 |  | Jerel | Or 40, or 40-50. Or 40 or 50 or 40 se-..., no [laughs] 40-60. |
| 1899 |  |  | Somethin' like that. |
| 1900 |  | R2 | Uh huh. 40-60. So you think, and 40-60, is that sort of close |
| 1901 |  |  | enough to be fair? |
| 1902 |  | C\&J | Uh huh. Um humh. |
| 1903 |  | R2 | Okay. Um, does it matter which numbers ... |
| 1904 |  | Jerel | If you playin' |
| 1905 |  | R2 | they can roll? |
| 1906 |  | Jerel | If you playin' with one dice, yeah. But if you was playin' with |
| 1907 |  |  | two, it would matter 'cause you can't get 1 , you can't get 1 when |
| 1908 |  |  | you playin' with two dice 'cause 1 is the first number, you can't |
| 1909 |  |  | roll [rolls two dice] you can't get number 1 like that. |
| 1910 |  | R2 | But like if you're only playing with one die, okay, would it matter |
| 1911 |  |  | whether you said Player A receives a point if, for example, Player |
| 1912 |  |  | A instead of getting 1, 2, or 3, got 2, 3, 4, and Player B had 1, 5, |
| 1913 |  |  | and 6? |
| 1914 | 6:42 | Chris | Yeah, that would've been fair, too. Of if he got odd and even |


| 1915 |  |  | numbers. |
| :---: | :---: | :---: | :---: |
| 1916 |  | R2 | That would, yeah? So what is it that's making it fair? |
| 1917 |  | Chris | The number of chances that you have to get the number. |
| 1918 |  | R2 | Oh, and in this case it'd have to be, what do you think it would |
| 1919 |  |  | have to be? |
| 1920 |  | Jerel | 3 and 3 people get 3 numbers and the other person gets 3 numbers. |
| 1921 | 7:05 | R2 | What about the second game? Do you remember the rules of the |
| 1922 |  |  | second game that you played? |
| 1923 |  | Chris | Yeah. |
| 1924 |  | Jerel | That we made up? |
| 1925 |  | R2 | Not the uh second game that you made up. You made up more |
| 1926 |  |  | than one fair game for the first game? |
| 1927 |  | Chris | [Nods.] We made up two games. We made up two games. |
| 1928 |  | R2 | Okay. What was the second one? |
| 1929 |  | Jerel | Oh no, not for this one [pointing at paper on the table], not for this |
| 1930 |  |  | one. |
| 1931 |  | Chris | We made up our own. |
| 1932 |  | R2 | Oh, okay. What about for the game with two dice? |
| 1933 |  | Jerel | Oh, two dice ... |
| 1934 |  | R2 | Tell me, tell me about that game. Tell me what, as it was stated, |
| 1935 |  |  | what were the rules of that game? |
| 1936 |  | Chris | It was, it was, the rules were um ... [turns over paper]. |
| 1937 |  | Jerel | If the, if the dice... |
| 1938 |  | Chris | landed on $2,3,4,10,11$, or 12, Player A woulda got a point and |
| 1939 |  |  | Player B woulda got zero. And if the dice land on 5, 6, 7, 8, or 9, |
| 1940 |  |  | Player B woulda got a point. |
| 1941 |  | R2 | And what did you think before you started playing it? Was, did ya |
| 1942 |  |  | think that this game was fair or not? |
| 1943 |  | Chris | Unfair. |
| 1944 |  | Jerel | It was unfair. |
| 1945 |  | R2 | Unfair. |
| 1946 |  | Chris | 'Cause Player A it had like, it had 3 small numbers, which are 2, 3, |
| 1947 |  |  | and 4, and you really can't get 'em. 'Cause right here we made a |
| 1948 |  |  | chart after ... |
| 1949 |  | Jerel | [Nudges Chris and points to his paper.] |
| 1950 |  |  | [The paper says: "The reason why the game isn't fair is because |
| 1951 |  |  | player B has a better chance has big numbers and Player A has |
| 1952 |  |  | small numbers." It then lists the numbers for Player A, labeling 2, |
| 1953 |  |  | 3 , and 4 as " 3 small" numbers and 10,11, 12 as " 3 big" numbers. |
| 1954 |  |  | Player B"s numbers, 5, 6, 7, 8, and 9, are labeled as "all big".] |
| 1955 |  | Chris | that 3 got one chance to get it, 2 got one chance, and, oh I didn't do |
| 1956 |  |  | 4. |
| 1957 |  | R2 | What? Let me see. Put you paper here just so I can see it. And |
| 1958 |  |  | explain to me what you're, what the idea is. |
| 1959 |  | Chris | Right here [pointing at paper], we put like how many times, how |


| 1960 |  |  | many ways can you get um each number. |
| :---: | :---: | :---: | :---: |
| 1961 |  |  | [The paper shows: |
| 1962 |  |  | $7=4+3,5+2,6+1$ |
| 1963 |  |  | $6=3+3,2+4,1+5$ |
| 1964 |  |  | $5=1+4,3+2$ |
| 1965 |  |  | $3=1+2$, |
| 1966 |  |  | $2=1+1$ |
| 1967 |  |  | $8=4+4,2+6,5+3$, |
| 1968 |  |  | $9=3+6,4+5$ |
| 1969 |  |  | $10=5+5,4+6$, |
| 1970 |  |  | $11=5+6$, |
| 1971 |  |  | $12=6+6$ ] |
| 1972 |  | Jerel | Like for this ... |
| 1973 |  | R2 | How many ways there are to roll each number? |
| 1974 |  | C\&J | Um humh. Yeah. |
| 1975 |  | Jerel | Like for 7 it was $4,4+3$ equals $7,5+2$, and $6+1$. For 6 it was |
| 1976 |  |  | $3+3,2+4$, and $1+5$. For 5 it was $1+4,3+2$. For 3 it was $1+2,1+1$ |
| 1977 |  |  | for 2. Eight for, was 4+4, 2+6, and 5+3. |
| 1978 |  | R2 | Um humh. |
| 1979 |  | Jerel | Nine was $3+6$ and $4+5$. Ten was $5+5,4+6$. Eleven was $5+6$. |
| 1980 |  |  | Twelve was $6+6$. And 4 was $2+2$ and $3+1$. |
| 1981 | 9:12 | R2 | And so why did you, why did you make this calculation? Why did |
| 1982 |  |  | you figure this out? |
| 1983 |  | Chris | Because after we played the game we realized that um Player B |
| 1984 |  |  | had, since it had larger numbers it had more chance of getting 'em. |
| 1985 |  | Jerel | And $7 . .$. |
| 1986 |  | R2 | Since the numbers were larger. |
| 1987 |  | Chris | Um humh. |
| 1988 |  | R2 | So what were the numbers that Player B on, would receive a point? |
| 1989 |  | Chris | $5,6,7,8$, and 9 . |
| 1990 |  | R2 | $5,6,7,8$, and 9 . |
| 1991 |  | Chris | Uh huh. 'Cause if you add up how many ways you can get 'em ... |
| 1992 |  | Jerel | [Interrupts.] Seven kept popping up. |
| 1993 |  | Chris | You got, for 5 you got 2, then you got, for 6 you had 3, then for 7 |
| 1994 |  |  | you had 3, for 8 you had 3, and for 9 you had 2 [writing these |
| 1995 |  |  | counts on the paper]. So if you add these up, you had 13 different |
| 1996 |  |  | ways to get your numbers. |
| 1997 |  | R2 | So Player B had 13 different ways of winning on a roll. |
| 1998 |  | Chris | Yeah. And Player A had, for 2 you only had 1 chance, for 3 you |
| 1999 |  |  | had 1 chance of getting it. Four you had 2 chances, 10 you had 2 |
| 2000 |  |  | chances, 11 you have 1 chance and 12 you have 1 chance [writing |
| 2001 |  |  | the counts on the paper]. So you got 8 . |
| 2002 |  | R2 | So, and is that what you thought at first, when you first read the |
| 2003 |  |  | game? |
| 2004 | 10:29 | Chris | I thought, when we first read the game, I thought ... |


| 2005 |  | Jerel | I thought it was fair. |
| :--- | :--- | :--- | :--- |
| 2006 |  | Chris | We thought it was fair because Player A had, well, it was still |
| 2007 |  |  | unfair but Player A woulda got more, woulda won. But after you |
| 2008 |  |  | played the game we saw that Player B started winning, so we just, |
| 2009 |  |  | um, thought that it was unfair and we figured it out. |
| 2010 |  | R2 | Uh huh. So, so let me see if I understand. When you first read the |
| 2011 |  |  | game, you thought that that Player A ... |
| 2012 |  | Jerel | Was gonna win. |
| 2013 |  | R2 | was more likely to win. |
| 2014 |  | Chris | Um humh. |
| 2015 |  | R2 | Um humh. Then you played the game and you found out that B |
| 2016 |  |  | was winning. |
| 2017 | $11: 00$ | C\&J | Um humh. |
| 2018 |  | R2 | Let's see. Where are the games you played where ... |
| 2019 |  | Chris | Right here. [C\&J point at the paper.] For the first game, Player B |
| 2020 |  |  | won, won 10 to 3. And right here we put the rolls of each one. |
| 2021 |  | Jerel | Seven kept coming up. |
| 2022 |  | Chris | Uh huh. Seven came up. For Player B it came out 5 times and for |
| 2023 |  |  | Player A it came out 3 times. |
| 2024 |  | R2 | So you're saying when Player B rolled, 7 came up 3 times? |
| 2025 |  | Chris | Five times. |
| 2026 |  | R2 | Five times. And when Player A rolled, 7 came up ... |
| 2027 |  | Chris | Three times. |
| 2028 |  | R2 | Three times. |
| 2029 |  | Chris | So 7 kept on popping up most of the games. |
| 2030 |  | R2 | Why did 7 come up so much? |
| 2031 |  | Chris | 'Cause it ... |
| 2032 | $11: 38$ | Jerel | Oh because it had a better chance, because it had 3 ways to get it. |
| 2033 |  |  | And that's why, if you can't, if you added them together, that's |
| 2034 |  |  | what kept coming. |
| 2035 |  | Chris | Um humh. So it's 5, 6, no, I mean, 7, 6, 7, 8 had 3 different ways |
| 2036 |  |  | of getting the numbers. |
| 2037 |  | R2 | I see, so that's what you're, you're saying here. So that's why you |
| 2038 |  |  | did this analysis is because you saw 7 came up so often? |
| 2039 |  | Chris | Um humh. |
| 2040 |  | R2 | And you wanted, so you did this to try to understand why 7 came |
| 2041 |  |  | up that often? |
| 2042 |  | Chris | Yep. |
| 2043 |  | R2 | And here you're saying you can roll a 7 if you have a 4 or 3. |
| 2044 |  | Chris | Um humh |
| 2045 |  | R2 | And, or a 5 and a 2, and a 6 and a 1. |
| 2046 |  | Chris | Um humh. |
| 2047 |  | R2 | And those are the different ways that it's po-, that you can obtain a |
| 2048 |  | Um humh. |  |
| 2049 |  | Chris |  |


| 2050 |  | R2 | Now, I see here [pointing at paper where Chris had just written the |
| :--- | :--- | :--- | :--- |
| 2051 |  |  | number of ways to get each sum] you're saying that this 2 refers to |
| 2052 |  |  | the number of times, which number? |
| 2053 |  | Chris | 5. |
| 2054 |  | R2 | Five appears. And this 3? |
| 2055 |  | Chris | 6. |
| 2056 |  | R2 | And this one? [pointing at 3] |
| 2057 |  | Chris | 7. |
| 2058 |  | R2 | Ah hah. But you're saying 6 is a, has 3 possibilities, and there are |
| 2059 |  |  | 3 possibilities of rolling a 7. Now, did you, did that come out for |
| 2060 |  |  | you experimentally when you played the game? That 6 also |
| 2061 |  |  | appeared... |
| 2062 |  | C\&J | [Nod in agreement.] |
| 2063 |  | Jerel | Yeah. |
| 2064 |  | R2 | More often? Did it appear as often as 7? |
| 2065 |  | Chris | No. [shakes head] |
| 2066 |  | R2 | How often did 6 appear? |
| 2067 |  | Jerel | Uh not uh ... |
| 2068 |  | Chris | Not as much as 7. „Cause when ... |
| 2069 |  | Jerel | The first game it appeared twice on my side and once on his side. |
| 2070 | $13: 12$ | Chris | And the second game it came out 1, 2, 2 times on his side and 1, 2, |
| 2071 |  |  | 3, 3 times on my side, uh on my side. |
| 2072 |  | R2 | Uh huh. |
| 2073 | $13: 21$ | Jerel | It wasn't as consistent as 7 was. It didn’t come, it kept coming out |
| 2074 |  |  | like this [tosses dice, apparently rolling a 7]. See? [waving his |
| 2075 |  |  | hand over the dice and smiling] |
| 2076 |  | Chris | 'Cause 7 in the second game, it came out 1, 2, 3, 4, 5, 6, 7 times. |
| 2077 |  | R2 | Um humh. |
| 2078 |  | Chris | And then, last time it came out 1, 2, 3 times. |
| 2079 |  | R2 | The 6? |
| 2080 |  | Chris | Um humh. |
| 2081 |  | R2 | Okay. |
| 2082 |  | Chris | No, the 7. |
| 2083 |  | R2 | The 7. So you're saying the 6 doesn't come up quite as often as |
| 2084 |  |  | the 7. |
| 2085 |  | Chris | No. |
| 2086 |  | Jerel | Even though it has 3, uh, ways to get it. |
| 2087 |  | R2 | Um humh. |
| 2088 |  | Jerel | Eight comes up a lot, though. |
| 2089 | $13: 53$ | R2 | If you were to play the game more often, say you played it 10 |
| 2090 |  |  | times, what do you think might happen in terms of the number of |
| 2091 |  |  | times 6 and 7 would come up? |
| 2092 | $14: 01$ | Jerel | It'd, it'd be a lot more. |
| 2093 |  | Chris | Um humh. |
| 2094 |  | Jerel | 15 to 20. |


| 2095 |  | R2 | Would they, would it be about the same or would 7 still come up |
| :---: | :---: | :---: | :---: |
| 2096 |  |  | more often? |
| 2097 |  | C\&J | Seven would still come up more often. |
| 2098 |  | R2 | Seven still come up more often. So, Chris and Jerel, there's |
| 2099 |  |  | something I don't understand. I'm a little confused here. You said |
| 2100 |  |  | here you have 7, there are 3 possibilities for 7. And Chris you said |
| 2101 |  |  | here there are 6 possibilities for 6,3 possibilities for 6 ? |
| 2102 |  | Chris | Um humh. |
| 2103 |  | R2 | So if you say that the number of possibil-, number of possible |
| 2104 |  |  | ways to obtain a 6 and a 7 are both 3 , why do you say that 7, it's |
| 2105 |  |  | more likely for 7 to appear if you were to play the game often? |
| 2106 |  | Jerel | [very quietly] Never thought about that. [louder] Maybe because |
| 2107 |  |  | [rolls dice], wait, let me see that. That was 7, right? Maybe |
| 2108 |  |  | because it takes, [pause] I don't know. |
| 2109 |  | Chris | 'Cause it takes more smaller numbers to make up, um the 6. And |
| 2110 |  |  | for 7 it takes like most, more large numbers to make up, make it |
| 2111 |  |  | up. |
| 2112 |  | R2 | I don't know what you mean. Will you explain that a little further? |
| 2113 |  | Chris | Like here, like say 1,2 , and 3 on the dice are the smallest numbers, |
| 2114 |  |  | like the smallest numbers or have the smallest. So 3 came out |
| 2115 |  |  | twice, 2 came out once, and 1 came out once. So you had two |
| 2116 |  |  | large numbers left. |
| 2117 |  | R2 | Um humh. |
| 2118 |  | Chris | So, but for 7 it had 3, 2, 1, three of 'em, and then 3 large numbers, |
| 2119 |  |  | so it had more possibilities again. |
| 2120 | 15:42 | R2 | So you're, let me see if I understand. You're saying that the, for 7, |
| 2121 |  |  | you have a 1, a 2, and a 3, and you call those the small numbers. |
| 2122 |  | Chris | Um humh. |
| 2123 |  | R2 | And they're more likely or less likely to appear over all? |
| 2124 |  | Chris | Less likely. |
| 2125 |  | R2 | Less likely to appear. And the 4, 5, and 6 are larger numbers and |
| 2126 |  |  | they're more or less likely? |
| 2127 |  | Chris | More. |
| 2128 |  | Jerel | [Has had his head down during this exchange.] More. |
| 2129 |  | R2 | More likely. Um, and so, tell me again about the 6 here. |
| 2130 |  | Chris | It had $3,3,2$, and 1 , which is four less likely to appear. |
| 2131 |  | R2 | Oh, so those are four less likely to appear numbers because those |
| 2132 |  |  | are smaller. |
| 2133 |  | Chris | And then two, 4 and 5 were more likely to appear numbers. |
| 2134 | 16:34 | R2 | Um humh. So the 7 has how many likely pairs, to appear numbers |
| 2135 |  |  | that come up when you ... |
| 2136 |  | Chris | Three. |
| 2137 |  | R2 | Uh huh. And the 6? |
| 2138 |  | Chris | That's 2. |
| 2139 |  | R2 | It's 2. That's interesting. So, and how do you know that the 4 and |


| 2140 |  |  | the 5, the 4, 5, and 6, are more likely to appear than the 1, 2, and 3? |
| :--- | :--- | :--- | :--- |
| 2141 |  |  | Or, is that on the roll of the die? |
| 2142 |  | Chris | [Nods] |
| 2143 |  | R2 | You're saying that they're more likely to appear? |
| 2144 |  | Chris | See, 'cause if you roll [rolls one die], got a 5, a 5, 6, 3. See, that's |
| 2145 |  |  | only once. And if you keep rolling [rolls again] 4, 3, twice ... |
| 2146 |  | Jerel | 6 |
| 2147 |  | Chris | Second time ... |
| 2148 |  | Jerel | I can maybe 'cause... |
| 2149 |  | Chris | Third time, fourth time. |
| 2150 |  | Jerel | Seven got one even number... |
| 2151 | $17: 27$ | R2 | Wait. Let's keep track of this, okay? Let's take a sheet of paper |
| 2152 |  |  | and keep track of how they're coming up. [Gives the boys a |
| 2153 |  |  | paper.] Who's gonna roll and who's going to keep record? |
| 2154 |  | Jerel | [points to Chris] Roll. |
| 2155 |  | C\&J | [Chris rolls die] 1, 4 |
| 2156 |  | R2 | How many times do you intend to roll? |
| 2157 |  | Chris | Uh, 10. |
| 2158 |  | R2 | Okay. |
| 2159 |  | Chris | 6, 2, 4, 1, 3, 1, 2, 6. [To Jerel] How much is that? |
| 2160 |  | Jerel | One is consistent. [Taps his pen on the paper as if pointing to and |
| 2161 |  |  | counting the rolls.] |
| 2162 |  | Chris | We did it 12 times |
| 2163 |  | Jerel | I know. |
| 2164 |  | R2 | Um humh. Okay. So what does this tell you? What does this |
| 2165 |  |  | experiment tell you? |
| 2166 |  | Jerel | That 1 came up a lot. One came up 1, 2, 3, 4, 5 times. |
| 2167 |  | R2 | Um humh. |
| 2168 |  | Jerel | And the other numbers came up 1, 2, 3, 7 times. |
| 2169 |  | R2 | Which other ones? |
| 2170 |  | Jerel | Like, 6 came up twice. |
| 2171 |  | R2 | Um humh. |
| 2172 |  | Jerel | Four came up twice. Three came up once and 2 came up twice. |
| 2173 |  | R2 | Now, does this experiment corroborate your original idea? |
| 2174 |  | Chris | No. [shakes head no] |
| 2175 |  | Jerel | [shakes head no] |
| 2176 |  | R2 | No. So, is it because of the way you threw the die, or ... |
| 2177 |  | Jerel | Yeah, wait a minute . . |
| 2178 |  | R2 | Or maybe you have to throw it more times? |
| 2179 |  | Jerel | When it landed on here [lifts mat from the table] it kept rolling to |
| 2180 |  |  | 7. Look. Well it kept rolling to 6 or something like that. [Places |
| 2181 |  | R2 | die on the mat.] 5 |
| 2182 |  | Was that, do you call that a roll, what Jerel just did? |  |
| 2183 |  | Chris | No [laughs]. |
| 2184 |  | R2 | That seemed like placing it down to me. |


| 2185 |  | Jerel | [rolls die] 1 |
| :--- | :--- | :--- | :--- |
| 2186 |  | Chris | [rolls die] 1 |
| 2187 |  | R2 | Are you keeping track? |
| 2188 |  | Chris | [rolls 1 off the mat and doesn't count it] 2, 6, 1 |
| 2189 |  | Jerel | [whispers to Chris] It's still low numbers. |
| 2190 | $20: 00$ | Chris | $5,5,4,6,1,5$. [The 5 was rolled off the mat, but counted.] How |
| 2191 |  |  | many times is that? |
| 2192 |  | Jerel | [counting silently] 10 |
| 2193 |  | Chris | It's fine [?]. Okay. |
| 2194 |  | Jerel | Well, all the numbers you can get 7 by. [Looks at R2 and smiles.] |
| 2195 |  |  | 'Cause 1+6, 2+ ... |
| 2196 |  | Chris | Four. |
| 2197 |  | Jerel | Yeah, 2+4. No, wait. [Turns and looks at Chris.] |
| 2198 |  | Chris | Oh, 4+3 |
| 2199 |  | Jerel | [To Chris] No, 5 + 2. There's 6+1, 5+2, 5+2, 4+3, 6+1, and 5+2. |
| 2200 |  |  | [taps paper with his pen] |
| 2201 |  | R2 | Oh, but I thought we were, you were talking about whether or not |
| 2202 |  |  | the 1, 2, or 3 is less likely to appear than 4, 5, 6. |
| 2203 |  | Chris | [Reaches for paper] The 1 appears... |
| 2204 |  | R2 | So what about this idea? |
| 2205 |  | Chris | [Circles the 1's and 2's on the paper. There were no 3's.] The 1, |
| 2206 |  |  | 2, or 3 appears 4 times, and the large numbers appear 6 times. |
| 2207 |  | R2 | So you have, you rolled the dice now, you rolled the die how many |
| 2208 |  |  | times so far altogether? |
| 2209 |  | Chris | Ten. Oh. [Writes "large numbers = 6", later changes this to 10.] |
| 2210 |  | Jerel | Oh, all 22. |
| 2211 |  | R2 | Okay, so what happened in this, these 22 trials? |
| 2212 |  | Jerel | Ummm, [pointing at paper] the first time little numbers kept |
| 2213 |  |  | coming up. |
| 2214 |  | Chris | Um humh. [Writes "small numbers = 10", later changes this to 12] |
| 2215 |  | Jerel | The second time all the big numbers came, like ... |
| 2216 |  | R2 | So if you combined this, if you combined the two trials? |
| 2217 |  | Jerel | The little numbers showed up more. |
| 2218 |  | R2 | Is that true? |
| 2219 |  | Chris | [writing on the paper] Let me check. |
| 2220 |  | R2 | And by little numbers you mean 1, 2, and 3? |
| 2221 |  | Jerel | [speaking at the same time] 1, 2, or 3. [Nods in agreement.] |
| 2222 |  | R2 | So how many times did a 1, 2, or 3 show up? |
| 2223 |  | Jerel | All together, the 1, 2, [inaudible] ... |
| 2224 |  | Chris | Ten, [inaudible] wait, counted wrong. |
| 2225 |  | Jerel | [counting while tapping the paper] Twelve times. And the large |
| 2226 |  | numbers showed up 10 times. |  |
| 2227 |  | Chris | Um humh. |
| 2228 |  | So what about your theory? The idea that you have. |  |
| 2229 |  | Well, what about when you roll with two dice? |  |


| 2230 |  | R2 | Before we go into the two dice situ-, two dice, what about this one |
| :---: | :---: | :---: | :---: |
| 2231 |  |  | die? Because you guys originally said that the lower numbers, 1,2 , |
| 2232 |  |  | and 3, were less likely to appear than the 4, 5, 6. |
| 2233 |  | Jerel | Yeah, but that was ... |
| 2234 |  | R2 | Do you still hold to that? |
| 2235 |  | Jerel | No. |
| 2236 |  | R2 | Chris? You don't look like you're sure. |
| 2237 |  | Chris | [Shakes head no] |
| 2238 |  | R2 | You're shaking your head meaning what? |
| 2239 |  | Chris | Don't know [smiling]. |
| 2240 |  | R2 | You don't know whether you want to revise your idea or whether |
| 2241 |  |  | you're going to stick with it? |
| 2242 |  | Chris | [shrugs his shoulders and makes a small giggle] |
| 2243 |  | R2 | You're not sure? |
| 2244 |  | Chris | [shakes head] |
| 2245 |  | R2 | So, what did this experiment tell you? |
| 2246 |  | Jerel | That the big numbers don't always show up. Like, when we |
| 2247 |  |  | played, it don't always show up. |
| 2248 |  | R2 | Um humh. So in the one, remember in the one die game? How |
| 2249 |  |  | did you make that game fair? |
| 2250 |  | Jerel | Um [laughs twice] |
| 2251 |  | R2 | Do you remember, Chris, what you told me? |
| 2252 |  | Jerel | Oh yeah, we, we gave each person 3 , 3 numbers. |
| 2253 |  | R2 | Um humh. And which numbers did you give to Player A? |
| 2254 |  | Chris | Player A, 1, 2, and 3. |
| 2255 |  | R2 | And to Player B? |
| 2256 |  | Chris | Player B, 4, 5, 6. |
| 2257 |  | Jerel | But that... |
| 2258 |  | R2 | And you call that a fair game. But I thought, but by your theory, |
| 2259 |  |  | that 1,2 , and 3 are less likely to appear, then it's not a fair game. |
| 2260 |  | Jerel | What? |
| 2261 |  | Chris | [shakes head] |
| 2262 |  | R2 | So I'm confused about what you're trying to tell me. |
| 2263 | 24:00 | Jerel | Now [sighing and smiling]. All right. I can make that a fair game. |
| 2264 |  |  | We give somebody 1,4 , and 5, and give the other person 2, 3, and |
| 2265 |  |  | 6. That'd be fair. You got two low numbers and one high number. |
| 2266 |  | R2 | Yep. That's fair. So it seems to me that this experiment somehow |
| 2267 |  |  | is causing you both to doubt your idea. Is that right? |
| 2268 |  | C\&J | Yep. |
| 2269 | 24:30 | R2 | Uh huh. Is there something you want to say about that? |
| 2270 |  | Jerel | Uh, nah. |
| 2271 |  | Chris | [shakes head] |
| 2272 |  | Jerel | I don't want to say nothin'. |
| 2273 |  | R2 | Well, you know maybe it would be interesting to think again about |
| 2274 |  |  | this problem involving both the one die and the two dice games so |


| 2275 |  |  | that you could come back maybe some other time to give me a |
| :--- | :--- | :--- | :--- |
| 2276 |  |  | better idea of what you're thinking about? |
| 2277 |  | Chris | [nods in agreement] |
| 2278 |  | R2 | To see whether or not things have changed or whether or not |
| 2279 |  |  | you're still holding on to the same set of ideas that you now have. |
| 2280 |  | Chris | [nods] |
| 2281 |  | R2 | Yeah? |
| 2282 |  | Chris | Um humh. |
| 2283 |  | Jerel | [nods] |
| 2284 |  | R2 | Okay. |

